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DEPARTMENT OF CHEMICAL ENGINEERING UNIVERSITY OF TILAWARE DELAWARE

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# LOCAL HEAT FLUX IN A VERTICAL DUCT WITH FREE CONVECTION IN OPPOSITION TO FORCED FLOW

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Submitted by: S. A. Guerrieri, relistant Professor of Commical Engineering-Russell J. Roma, Research Fellow in Chemical Engineering

Department of Chemics: Ungineering
University of Delaware
Newark, Delaware

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#### SUMMARY

Heat transfer rates accompanying simultaneous natural convection and forced flow of air in a vertical channel, using an optical method, were studied experimentally, under conditions such that the two types of flow tended to oppose each other. Thus the light, heated air tended to flow upward near the vertical surfaces of the channel while the air stream as a whole was forced to flow downward. These conditions are qualitatively similar to those occurring in cooling passages inside blades of gas turbines.

Optical measurements showed that natural convective flow predominated at low forced-flow velocities and high temperature differences while at high mean velocities the flow was downward even at the wall. Under intermediate conditions a maximum rate of heat transfer occurred about half-way up the channel, owing to instability of the laminar flow associated with the opposing forces. At the highest mean velocities the local heat transfer coefficients agreed closely with values expected from laminar-flow theory neglecting natural convection.

#### INTRODUCTION

Two important types of fluid flow problems involving heat transfer are those of forced and those of free convection. Forced-convection flow is maintained either mechanically through a pressure drop or by means of hydrostatic head or by both. Free-convection flow, on the other hand, is caused by differences in the hydrostatic pressure of a fluid due to density differences because of temperature differences. Heat-transfer coefficients for the standard cases of forced and free convection are usually calculable by well known empirical and theoretical equations.

Flow produced by both free and forced convection forces simultaneously have now become of practical importance. Many sircraft propulsion systems contain components in which heat is being transferred. Free-convection flow due to density gradients is superimposed on the forced flow through helicopter ram jets and on the flow of air in the cooling passages in the blades of turbines. As will be seen, this can appreciably influence the resultant flow and heat transfer.

The present paper presents the mechanism and result of simultaneous action of forced and free convection forces on heat transfer when such forces are in direct opposition to each other. Data were taken in the range in which forced and free convection forces were of the same order of magnitude.

#### APPARATUS DESCRIPTION

The test unit was a vertical rectangular duct. Air was forced down through the duct while heat was supplied to two particular areas and caused a buoyant force in opposition to the pressure drop.

The sectional end view of Figure 2 shows the construction of the duct which can be considered to have been assembled in the following manner. Two machined and polished, rectangular, 1/2-inch aluminum plates, 8" x 12" formed the heating surface. These were held 1.01" apart, parallel and with the 12" axis vertical. Sides were put on these plates to form a vertical duct, open at both top and bottom. A side consisted of an aluminum frame which held a piece of plate glass 12" x 1-1/6". Between the frame and the aluminum heating plates there was placed a 1/2-inch wide strip of 1/16" Buna-S rubber, a 1/2" deep x  $1/2^n$  wide transite insulation strip, and a  $1/2^n$  wide layer of glass cloth impregnated with Permatex No. 2. materials extended at least the vertical length of the heating plates. A cross section of this is seen in the top view of Figure 2. Note that a beam of light passing parallel and adjacent to either heating plate would not touch these materials since they were recessed slightly.

Calming sections were attached to both top and bottom of the heated duct. Cross sections of both were 9.75" wide x 1.04" deep. The top calming section was 24-1/2" in length, the bottom, 8-1/2". Connection was made by means of a thin extension of the heating plates to meet a similar extension in the calming duct sides. These extensions were overlapping, but were separated by means of a 1/4" slab of transite insulation. Connection was made through the 1/4" transite slab by means of 8 stud bolts per side. A short adjustable side was put in the connection between the end of the window

frame and the top calming section. A 1/4" foam rubber gasket plus the movable nature of this piece made possible a correction for differences in thermal expansion. Design of the entire duct was such that the inside dimensions were the same at any point down the duct, with the exception that the distance between the heating plates was 1.01" while the distance between the corresponding faces of the calming sections was 1.04" wide.

Wall temperatures in the heating plates were measured by means of L & N No. 30 B&S glass insulated iron-constantan Duplex thermocouples. These couples were located in horizontal holes which were drilled parallel to and 1/4" from the heat transfer interface. This gave the junction and wire leading to it a 4" isothermal zone in the plate. These thermocouples were located at a distance, x, from the top of the heated plate of 1, 3, 5, 7, 9, and 11 inches.

At the top and bottom of the duct, mechanisms supported a travelling thermocouple which could move anywhere in a plane perpendicular to the heated surface and passing through the axis of the duct. The mechanism of movement could determine horizontal changes in position of the junction within 0,0005" and vertical changes within 1/16". Figure 2 shows the construction.

The travelling thermocouple itself was made by butt silver soldering L&N No. 40 B&S (.0031") copper-constantan bare thermocouple wire. The couple was gold plated for 1" on the copper side of the junction and 3/8" on the constantan side of the junction. This plating and subsequent polishing were done in order to minimize radiation error.

All thermocouple wires led into insulated switch boxes. Separate boxes were used for the copper-constantan and iron-constantan connections. Leads to the potentiometer were

combined through a small switch in one of the boxes. The resulting connection led to a No. 2732 Rubicon Potentiometer. Cold junctions for both the copper-constantan and iron-constantan couples were maintained in the same ice bath in a kerosene filled 1/2" glass tube immersed 8" in a thermos jug of ice-water.

Air was supplied by means of a GE Model No. 150 centrifugal blower. Air passed horizontally from the blower to a sharp right angle bend and then up three feet of 2" brass pipe to a section where a sharp edged orifice was installed. Pipe taps one diameter up and down stream served as both pressure taps for the orifice meter and inlets for thermocouples. A manometer, using air over water, was used to measure the pressure differential across the orifice plate. After another foot of brass tube, the air passed through a 3/4" hose to the top of the flow distributor. distributor served as a housing for the top thermocouple mechanism and as an energy converter for the incoming gas. The air then flowed down through the top calming section and through the heated section of the duct. A narrow slot was formed 1/4" below the heated plates by means of strips of light sheet metal extending inward from each wall. The width of the slot was 0.41" except for a small slit at the center to permit the travelling thermocouple to reach the wall. construction can be noted by reference to the top and side sectional view of Figure 2.

Tubes were soldered to the outer wall of both the top calming section and the window frames. A controlled flow of water through these tubes maintained the sections at room temperature.

Onto the two outside surfaces of the heating plates were attached 8" x 12" plates of 1/2" thick aluminum. Six equally

spaced 350-watt GE strip heaters were mounted horizontally on each plate spacing. It was therefore necessary for heat produced in the strip heaters to pass through one full inch of aluminum plate in order to gain the inside air-interface surface; thus uniform distribution of heat was assured. These strip heaters were connected in parallel in banks of three, two banks to a side. Power was supplied to these banks individually as shown in the wiring diagram presented in Figure 3. This consisted essentially of a variable voltage transformer between the line and each bank. An additional circuit was added to enable a wattmeter to be thrown in between the transformer and the heater.

The optical apparatus set-up is best described by reference to Figure 4. Light produced by a DC arc lamp was focused on a stop by means of a Taylor-Hobson  $6\frac{1}{2}$ " f/2.5 lens. The stop contained an 0.015" diameter pinhole, which permitted passage of some of this light. The smallness of the hole permits consideration of the light as coming from a point source. The light then passed to an 8" parabolic mirror which was located at its focal distance (50") from the pinhole. reflected light from the parabolic mirror was substantially parallel and horizontal. A small angle (3.2°) between the incident and the reflected light means a negligible distortion. Due to the small refraction of the light rays passing through the test unit it was necessary to have a long optical path beyond the unit. Since the room in which the experiments were conducted was not as long as desired, it was necessary to use two plane, front-surface mirrors to extend the optical path. At the point at which the focus of the refracted rays was desired, an 8" x 10" photographic plate was installed. A  $3\frac{1}{5}$ long wooden rectangular duct extended from the plate toward the light source to protect the photographic plate from stray light.

A shutter was installed just beyond the pinhole, to permit a known exposure time on the negative. Film used was Kodak Contrast Process Ortho.

The parallel beam optical path to the test unit was an 8" diameter circle. However, the test section of the test unit was 12" high. Since the optical system once aligned, was very difficult to adjust for accurate work, it was made as a stationary installation. Then, in order to use optical methods on the entire test unit, it was necessary to arrange for vertical revement of the test unit. The unit was, therefore, suspended on a frame in which it could be moved up or down. The weight of the unit was counterbalanced by 128 lbs. of iron sash weights.

A triangular arrangement of three jacks at the base of the supporting framework permitted adjustment of the test rig to vertical. A plumb bob, suspended from an arm, high on the outside of the duct, was used to determine vertical alignment. Near the bottom, the wire supporting the bob passed through a ring. The duct was considered to be vertical when the wire supporting the bob was centered in the ring.

#### PROCEDURE

The test unit was initially put into operation by supplying power to the blower and heating elements, and cooling water to the cooling tubes for the window frames and top calming section.

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About two hours were required for the unit to come to equilibrium which was determined by temperature equality of opposite heating plates, constant wall temperatures, constant inlet air temperature (inlet air was heated by the blower), stability of pressure drop across the sharp edge orifice in the air supply line, and approximate room temperature for the water cooled sections.

After attainment of equilibrium, the test unit was aligned vertically and optically. Vertical alignment was accomplished by changing the length of three jacks supporting the frame so that the plumb bob wire was centered in the ring. The test unit was finally readied by aligning both the parallel incident light and the traveling thermocouple in planes parallel to the heating surfaces.

Traveling thermocouple data were first taken. The junction and wire were first located parallel to the surface at either y = 0.005" or y = 0.0075" from the surface. The junction was then moved vertically down and readings were taken at various values of x inches from the top. A new plane further from the surface was next chosen, and the procedure repeated and so on. The last plane chosen was at y = 0.500" which was close enough to the center to be called the centerline. Actual centerline was at y = 0.505". Only data from one wall to the centerline were collected. Temperature distribution in the gas on the other side of the centerline was assumed to be symmetrical.

All wall temperatures of the heating plate were taken

on the side which was used as the datum plane for the traveling thermocouple. As a check on the opposite side, one wall temperature was taken there for comparison.

Pressure readings were taken across the orifice and between atmosphere and the downstream orifice top. Thermocouples installed at the pipe taps gave temperatures at these points. Finally barometric pressure was recorded.

With lights out, the arc lamp was turned on and pictures were taken of refraction occuring in the lower half of the test section. The test unit was then lowered and similar pictures were taken of the upper half of the test section. Usually two pictures, of 1/5 and 1/2 second exposure time, were taken of each section. Standard procedure was used in development of the negatives.

#### DISCUSSION

Outline of the Problem. Interest is centered on heat transfer to a fluid forced to flow through a conduit in which gravitational or centrifugal forces are in the direction of the flow.

The temperature gradient from the heated surface to the main body of the fluid produces a change in density in the direction normal to the flow of fluid. The gravitational or centrifugal forces acting on this change in density, produce a difference in hydrostatic head across the conduit. The less dense material near the heated surface, therefore, has less hydrostatic head than the fluid near the center of the duct. Since the fluid pressure normal to the flow is essentially constant across any cross section, this difference in head causes an unbalance of forces, and depending upon the relative strength of these forces, results in reduction, stagnation, or reversal of the downward flow of fluid near the wall.

Since it was not practical to have a simple test unit in which the accelerative force was produced by centrifugal force, the unit had to be so arranged that gravity acted as the effective total of all constant accelerative forces. In the problem under discussion, this was arranged by having a vertical duct as the test unit.

Exact Theoretical Equations. The theoretical equation for heat flow to a moving fluid (1) can be expressed as follows:

$$\frac{\partial t}{\partial \theta} + u_x \frac{\partial t}{\partial x} + u_y \frac{\partial t}{\partial y} + u_z \frac{\partial t}{\partial z} = \alpha \left( \frac{\partial^2 t}{\partial x^2} + \frac{\partial^2 t}{\partial y^2} + \frac{\partial^2 t}{\partial z^2} \right) + \frac{\alpha}{\rho c} (1)$$

The velocity terms in Equation 1 can be expressed by Newton's law, Force = Mass x Acceleration. Newton's equation, applied to motion of unit volume of the fluid in the direction of three coordinates, respectively, (2) becomes:

$$\rho \frac{du_{x}}{d\theta} = (g_{x} + P_{x} + F_{x}) \varepsilon_{c}$$
 (2)

$$\rho \frac{du_{y}}{d\theta} = (\varepsilon_{y} + P_{y} + F_{y}) \varepsilon_{c}$$
 (3)

$$\rho \frac{du_z}{d\theta} = (g_z + P_z + F_z) g_c \qquad (4)$$

where the total force is composed of:

- 1. Inertia forces  $g_x$ ,  $g_y$ ,  $g_z$ , as gravity, or centrifugal force.
- 2. Dynamical forces Px, Py, Pz, as the pressure drop.
- 3. Frictional forces  $F_x$ ,  $F_y$ ,  $F_z$ , caused by viscosity and well friction.

Frictional forces (F) are expressed in the equations of Stokes (3):

$$F_{x} = \mu \left( \frac{\partial^{2} u_{x}}{\partial x^{2}} + \frac{\partial^{2} u_{x}}{\partial y^{2}} + \frac{\partial^{2} u_{x}}{\partial z^{2}} \right) + \frac{\mu}{3} \frac{\partial}{\partial x'} \left( \frac{\partial u_{x}}{\partial x'} + \frac{\partial u_{y}}{\partial y'} + \frac{\partial u_{z}}{\partial z'} \right)$$
(5)

Two similar equations (denoted as Eq. 6 and Eq. 7, respectively) for F and Fz follow by cyclic variation of x, y, z, and  $u_x$ ,  $u_y$ ,  $u_z$ .

Exact solution would require simultaneous solution of Equations 1 to 4. However, it is obvious that analytical solution of Equations 1 to 4 is impossible. For practical

purposes, considerable simplification of these equations can be attained without great loss of accuracy. Such simplifications, however, must include laminar flow.

Approximate Theoretical Equations. For the heat conduction equation, Equation 1, such simplifications include the assumption of:

- 1. Steady state unidirectional laminar flow.
- 2. Constant physical properties of the fluid  $(\mu, c, \rho)$ , and k).
- 3. Negligible conduction in the direction of flow, i.e. in direction x.
- 4. Temperature independent of time.
- 5. Constant duct wall temperature

Application of these assumptions give:

$$u_{x} \frac{\partial t}{\partial x} = \alpha \left( \frac{\partial^{2} t}{\partial y^{2}} + \frac{\partial^{2} t}{\partial x^{2}} \right) \tag{8}$$

For the hydrodynamic equations, Equations 2 to 7, such simplifications are:

- 1. P and F are negligible in the direction y and z.
- 2. Physical properties of fluid are constant with the exception of the density in relation to g, the acceleration due to gravity.
- 3. Flow is constant and unidirectional
- 4. Gravitational or centrifugal force lies in the x direction only.

Application of these assumptions to Equations 2 to 7 give:

$$g_{x} + P_{x} + F_{x} = 0 \tag{9}$$

and 
$$F_x = \mu \left( \frac{\partial^2 u_x}{\partial y^2} + \frac{\partial^2 u_x}{\partial z^2} \right)$$
 (10)

Since  $P_x = -\frac{\partial p}{\partial x}$ , and  $g_x = \frac{g_L}{g_C} \rho$ , the hydrodynamic

equation becomes:

$$\frac{\partial p}{\partial x} = \frac{g_L}{g_C} \rho + \mu \left( \frac{\partial^2 u_x}{\partial x^2} + \frac{\partial^2 u_x}{\partial z^2} \right)$$
 (11)

Changes in density are manifest by a change in velocities due to expansion of the fluid and by a change in the gravitational or centrifugal force on a unit volume. Since the former effect has been held constant and the latter has been regarded as a function of temperature, we find that Equations 8 and 11 offer practically the furthest theoretical simplification of the actual case as stated under "Outline of the Problem". Some additional simplification results for the case of flow through a cylindrical tube or between flat parallel plates of infinite extent. But, nevertheless, simultaneous analytical solution of Equations 8 and 11 does not appear possible.

For analytical solution of Equations 8 and 11, it is necessary to regard the density as constant also.

In this case then  $\frac{\partial P}{\partial x} - \frac{g_L}{g_C} \rho = \text{Frictional Pressure Drop.}$ So Equation 11 can be expressed as:

$$(\frac{\partial p}{\partial x}) = \mu \left( \frac{\partial^2 u_x}{\partial x^2} + \frac{\partial^2 u_x}{\partial z^2} \right)$$
 (12)

Solution of Equation 12 for flow in cylindrical tubes or between flat parallel plates of infinite extent results in a parabolic velocity distribution (4). Substitution of the parabolic velocity distribution in the heat conduction equation, Equation 8, results in equations amenable to solution.

Norris and Streid (5) have compiled and plotted these solutions for the cases of parallel infinite plates and circular tubes. A plot of these equations is given in Figure 12. Coordinates are listed in Table 12. The heat-transfer coefficients used are defined by Equation 13.

$$\frac{q}{A} = h_{a} / t_{w} - \frac{t_{2} + t_{1}}{2} / = h_{1} / t_{w} - t_{1} / T_{w} - t_{2} / T_{w} - t_{1} / T_{w} - t_{2} / T$$

<u>Previous Experimental Work.</u> Stender (6) investigated the heating of upward or downward flowing water in a vertical pipe. Flow rates were between a Reynold's Number of 10,000 and 68,000. Little difference was found between heat transfer rates with flow in either direction. He concluded, therefore, that the buoyant force had negligible effect beyond  $N_{Re} = 10,000$ .

Jurgensen and Montillon (7) heated water flowing within a vertical tube and found the heat transfer coefficient independent of flow direction for  $N_{Re}$  greater than 20,000. Between the lower limit of investigation ( $N_{Re} = 8,000$  to  $N_{Re} = 20,000$ ) they noted that downward flow gave higher coefficients than either upward flow or flow within a horizontal pipe. Within this range their data for heating water in downward flow in a vertical tube are correlated by:

$$N_{Hu} = 0.41 \, H_{Re}^{0.54} \cdot N_{Pr}^{0.40}$$
 (14)

They also mention that Scennecken, (8), who built and first used the apparatus used by Stender, reported higher coefficients with downward than with upward flow.

Colburn and Hougen (9) found that, for heating water flowing in a vertical pipe at rates up to  $N_{\hbox{\scriptsize Re}}$  of 2200, the data for that particular tube are correlated by:

$$h = .42 t (\Delta t_a)^{1/3} \quad \text{for upward flow}$$
 (15)

$$h = .49 t (\Delta t_a)^{1/3}$$
 for downward flow (16)

Experimental Approach to the Problem. Preliminary consideration indicated that if flow rates were low, the fluid could become buoyant enough in the vicinity of the will to rise against the direction of flow. Under such considerations it was noted that the heat-transfer coefficient may be a function of length and Grashof Number (10) as well as the variables expressed in equations of former work (N<sub>Re</sub>, N<sub>Nu</sub>, N<sub>Pr</sub>). Therefore, it was felt highly desirable to determine local heat transfer coefficients.

One method of determining local coefficients is to obtain the temperature gradient at the wall. Since at the wall the velocity is zero, the heat transfer is by conduction and can be expressed as.

$$\frac{\mathbf{q}}{\mathbf{A}} = 12\mathbf{k}_{\mathbf{W}} \left( \frac{\partial \mathbf{t}}{\partial \mathbf{y}} \right)_{\mathbf{y} = 0} \tag{17}$$

when the gradient is expressed in degrees F. per inch.

If the flow rate of the fluid is not too great, then a linear velocity gradient exists for some distance from the wall. McAdams (11) presents data for air in isothermal

flow, in which the linear velocity gradient extends 0.10 inch from the surface for an average velocity of 7 ft. per second. This distance incresses as the velocity decreases.

Martinelli and Boelter (12) give Leveque's solution to the heat conduction equation (Equation 8) for the case of heat transfer to a fluid which has a linear velocity gradient from the heat transfer surface. Their plot of this solution shows that the temperature gradient, too, is essentially linear from the wall.

It is apparent, then, that the temperature gradient at y = 0 extends out into the fluid for some distance in cases of low flow rates. Since the velocities at which the buoyant force causes an effect on heat transfer are in the low Reynold's Numbers anyway, this approach should be valid for this investigation.

At least two methods are available for finding the temperature gradients at the wall. One method is to take thermocouple readings at known distances from the wall to find the slope directly. The other is by means of the amount of refraction of light which was initially parallel to the heated surface. Both methods were used and found successful.

Besides these methods, the mixing-cup temperature of air into and out of the heated section was taken as further check. Separate descriptions of each method follow.

#### Heat Transfer from Traveling Thermocouple Measurements

The hot junction of the traveling thermocouple is adjacent to air at one temperature and essentially surrounded by a heated duct at another. These temperature differences can become appreciable, and the heat transferred to the wire by radiation will cause the wire to be at a higher temperature than the surrounding gas. Since the wire measures its own temperature, this error is introduced in gas temperature measurement.

The radiation error can be calculated by setting up a heat balance around the wire. Heat to the wire by radiation will be equal to heat leaving by convection if the wire is in an isothermal plane. Since the couple is inclosed by a virtual black body, we have:

quadiation = qconvection

$$0.173 \text{ CLá}^{*}((\frac{T_W}{100})^{\frac{1}{4}} - (\frac{T_{\text{wire}}}{100})^{\frac{1}{4}}) = h_{\text{x}}\text{CL}(t_{\text{wire}} - t_{\text{gas}})$$
 (18)

Original calculations were made for:

T = 1060 °R (600°F)

Twire 660 °R (200°F)

a" = 0.84 for oxidized constantan

h\_ = 60 (see Ref. 13)

and resulted in

•

twire tgas = 26 °F

To reduce this error, gold was plated on the junction and polished.

Then, 
$$a'' = 0.035$$
  
and  $t_{wire} - t_{gas} = 1.1$  °F

0

However, the introduction of gold onto the surface of the copper to constantan junction causes an additional electromotive force effect. Essentially, a new junction is established between the gold and constantan. The copper to gold plate contact seems to have negligible effect.

Application of a heated rod of known temperature over the point at which the gold plate stopped on the constantan side of the junction indicated that a calculated (14) temperature gradient of 50 degrees F. per inch gave an emf error of about 10 degrees F.

It was then necessary to obtain the length of the gold plate on the constantan side of the junction which would cut down the radiation error at the true junction, and yet be short enough that both major and minor junction had essentially the same environment temperature.

In order to calculate the length of plate needed for this condition, the point at which gold plate stopped on the constantan side of the true junction was considered to be attached to a solid wall of temperature 26 degrees F. (umplated wire to gas At). The wire then extended out into an environment of temperature 1.1 degrees F. (minimum protected wire At). The solution for this case (14) gives the temperature at any point along the wire.

The final solution of the problem then rests as a belance between the length of plating which will reduce

the error of radiation from 26 °F to "t", versus the distance between the junction and psuedo-junction which will raise the error from 0 °F to "t". This length proved to be 3/8" on the constantan side the junction, which results in an estimated error or about 3 °F.

On the copper side of the junction there appeared to be no error introduced by the gold plate; and so the plating was extended far enough to reduce the error theoretically to 1.2 degrees F. This length was 1" on the copper side of the junction. Total length of gold plate was therefore 13/8".

The copper constantan wire used for the traveling thermocouple was Leeds and Northrup No. 40 B&G Gauge (0.0031"). The small size minimized error due to conduction when the wire lay in a non-isothermal plane. To obtain a point junction and yet have both joined wires on the same axis, the junction was made by butt silver-soldering. This was accomplished by dipping 1/8" of the end of each wire to be joined into a molten drop of low melting point silver solder. These two ends were then accurately butted by means of a micropositioner. A small flame (1/8") was touched to the junction and the silver-solder flowed into the slight gap to form a continuous wire. Flux was used in all soldering operations. So successful was this method that in some of the couples made, it was not possible to tell exactly where the junction lay without a low power microscope since color was obscured for 1/8" on either side of the junction due to the silver coat.

Gold plate was applied by using a 1-volt potential for about 20 minutes. The area which rested in the plating solution but which was not to be plated (only the distance of 1 3/8" was to be plated) was protected by a coat of

Wonder-Las stop-off lacquer.

0

Two different traveling thermocouples were used in the course of all runs. One had a small bead (estimated thickness of  $0.00\mu^{\text{M}}$ ) which identified the junction. The position of the junction of the other could be identified only because its distance from the end of the gold plate on the constantan side of the junction was known.

Slight differences in temperature between the two heated plates or between opposite sides of the top calming section shifted the calming sections slightly from vertical parallel to the heating surfaces. If the traveling thermocouple was flush with the heating surface at one set of conditions, it was found that it might have been displaced 0.020% in the next. Such variation made it desirable to zero the traveling thermocouple before each run.

To zero the thermocouple was not difficult. If the thermocouple wire was close to the heating surface and light was directed at a small angle to the heating surface, then the shadow of the wire on the surface as well as the wire itself could be seen. It can be shown geometrically that the distance between the images as seen is twice the actual distance from wire to plate. Under these conditions the wire can be located with reference to the surface within several thousandths of an inch.

In operation it was found that the wire, although originally parallel to the surface, would not necessarily be parallel when the junction was moved vertically. Fortunately, however, the junction stayed a fixed distance from the wall.

Actually, the error in measure of the distance between the wall and the wire was not critical, since the temperature gradient was taken by moving a fixed horizontal distance from some reference point near the wall. It made no difference in calculations whether an attempt was made to fix a standard reference point.

As indicated in "Procedure", at particular points, x, down the heated duct four temperatures were taken at specific intervals away from the heating surface.

Temperature measurements taken by means of the traveling thermocouple were less accurate the farther from the wall the junction was located. At 0.005" from the wall the galvanometer was very steady. The farther away the couple was placed, the more the galvanometer oscillated. In some cases, duplication of results could not be secured within 0.2 millivolt for y = 0.10" from the wall.

Despite this error, slopes were easily found by use of the four points. Cases in which the error was large due to the eddying of the gas were cases of large temperature gradients anyway and the percent error was approximately the same in all.

Temperature measurements for gradients near the start and end of the heating section  $(x = 0, 11.75^{\text{M}})$  were the most in error. At the start of the heating section, the temperature measurements gave a curve up to the wall. The gradient at this point was estimated and is listed in the data (Table VIII), but was so obviously in error that the gradient as determined by the optical method was substituted for calculation of the heat flow. Near the end of the heated plate  $(x = 11.75^{\text{M}})$ , the disturbance due to the sontraction (located  $1/2^{\text{M}}$  farther down) as well as

a drop-off of plate temperature due to conduction to the lower calming section, seemed to cause peculiar results. With these exceptions results were good.

As expressed in Equation 17, the heat transfer rate per unit area is known if the temperature gradient in air at y = 0 and the thermal conductivity are known. To find the total heat to the air it is necessary also to define the area of heating surface from which this heat passes.

The length of the heating plates which was 12", is defined as the heated length. The width of the heating plates was 8". At the edges, however, there was a 1/2" transite strip and a 1/16" rubber gasket through which the temperature dropped from t, to the cooled-windowframe temperature (about room temperature). The heating width was therefore approximately the eight inches of aluminum plate plus one-half of the distance through the transite-gasket insulation on each extreme or 8.56".

It was assumed that the point temperature gradients as found at the center line existed across the heated width. Under this assumption, the average temperature gradient is expressed as:

$$\left(\frac{\partial t}{\partial y}\right) = \int_{0}^{L} \left(\frac{\partial t}{\partial y}\right) \frac{dx'}{L'} \tag{19}$$

For this integration, the gradients  $(\frac{\partial t}{\partial y})$  were plotted versus x(but the temperature gradient at x = 0 was taken from the optical data). The resulting graph was then integrated by using Gauss's 6 point fintegration formula (15). Then:

$$q = 12 \pm_{W} \Lambda \left( \frac{\partial t}{\partial y} \right)_{R} \tag{20}$$

where  $(\frac{\partial t}{\partial y})_{q}$  is expressed in degrees per inch. A in this case is 2 x 8.56 x 12.00/144, = 1.425 sq. ft.

Values of the temperatures from which temperature gradients were calculated, temperature gradients, and Q<sub>t</sub> calculated from these gradients, are listed in Tables III. VIII, and X, respectively.

#### Heat Transfer from Visual Measurements

Jakob (16) points out that if a heated plate in air has a constant temperature gradient from the surface for a short distance, then the refrection of a grazing beam of light over this surface can be used to measure the temperature gradient. We have already noted, in the flow range to be studied, that a linear temperature gradient exists for some distance from the wall into the fluid. The method then appears ideal for the present study.

Martinelli et al. (17) outline the mathematical derivation of the equation for calculation of the temperature gradient from amount of refraction:

$$\left(\frac{\partial \mathbf{t}}{\partial \mathbf{y}}\right) = \frac{\mathbf{y}_{\mathbf{s}}^{\mathrm{T}}\mathbf{w}}{0.1448} \frac{760}{P_{\mathbf{b}}^{\dagger}} \frac{1/12}{\mathbf{s}_{\mathbf{h}}^{\mathrm{L}}_{\mathbf{qpt}}}$$
(21)

where  $\beta$  is a correction factor which effectively replaces  $T_{w}$  by an average temperature through which the light passes in the course of refraction, and is expressed by the equation:

$$\beta = 1 + \frac{0.31}{.144} \left(\frac{Y_8}{L_{opt}}\right)^2 \frac{760}{P_b} T_w$$
 (22)

The test unit as described under "apparatus" comprised a flat duct with two parallel, opposite heating surfaces as the wider sides, and glass windows as the narrower. With two parallel plates, the obvious me hod of obtaining grazing light is with parallel light. Figure 4 shows the equipment arrangement to obtain parallel light.

Idealized operation of the test unit for visual purposes is best noted by reference to the lower right hand view on Figure 5. This view presents the test duct as if looking down from above. Air is passing into the plane of the paper. Light which is originally grasing and parallel to the heated surface is refracted from the heated surface. After leaving the duct the light resumes a linear path, but with the deviation it had upon leaving the test unit. A screen is set up beyond the test unit to intercept the refracted light. The distance is measured between the point at which this light falls upon the screen after passing by the heated plate, and the point at which it falls if no heat is applied to the unit (no deviation). Since the distance of the screen from the test unit is known, the temperature gradient throughtwhich this grazing light passes can be calculated from Equation (21).

The main graph of Pigure 5 shows the amount of refraction of the light in relation t the temperature through which it passes. The solid, arrow marked lines indicate light which has just left the test unit ("Emergence of Light from Test Unit"), after having passed perpendicular to the dotted temperature profile shown under the main diagram.

The refraction of the light beam, such as beam AA, which just grazes the heated surface is of interest. Its distance of refraction on the screen is measured from a linear extension of the heated surface to the indicated point. Total distance of refraction is Y<sub>s</sub>. Note however, that beam BB which initially was parallel but not adjacent to the heated surface was refracted even more than beam AA. This was caused by the fact that beam BB has passed through the same temperature gradient, but at a lower absolute temperature than beam AA. Review of Equation 21 will show that this condition is expected to give a larger refraction.

Beam CC, which is typical of light passing through the center of the duct, is refracted little because of the low temperature gradient. These beams form a bright center line on the screen.

Example of these patterns of refraction can be noted by reference to Figure 6, Run E-4.

If the screen is brought to within 2 to 5 feet of the test unit, the convergence of rays BB and CO indicate closely the point of actual penetration of heat to the gas. In some cases also it is a measure of a laminar film. In all cases, the refraction is so slight at this distance, that the image as seen gives essentially the actual distance between heated films. Figure 8 shows rull size pictures of such "élose-up" for the upper and lower section of the test unit.

Due to the lack of linear length beyond the test unit, it was necessary to install two plane front-surface mirrors. Since the standard front-surface mirrors are not optically plane, it was necessary to correct for deviations.

After exhaustive tests, it was found that horizontal deviations were negligible. Vertical deviations, however, resulted in a 1/4" contraction of the image. Correction of this problem rested on placement of a "ladder" in front of the test unit window. This ladder had rungs which cut off the entering light at known intervals down the heated length. The resulting photographs then had these markings which located exactly where the light had come from. This procedure also helped correct for vertical refraction.

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In some cases, it was desirable to put a stop in the light path to cut out all of the light which would otherwise have passed through the center of the duct, (such beams as CC in Figure 5). Only a vertical slab of light 0.07" thick and adjacent to each heated surface was permitted to pass across the duct. Figure 7 shows photographs taken with and without the stop.

As noted in the section headed "Apparatus", it was necessary to move the test unit up and down since the unit was greater in vartical length than the height of the optical path; the parabolic mirror was only 8" in diameter whereas the length of the test unit used for pictures was from x = 0 to 11.75. Therefore, it was necessary to readjust the position of the unit for each run, and to realign the heating surfaces parallel to the parallel light. However, such alignment was not difficult. If parallel light was passing between the two polished parallel plates in the test unit, and the plates were turned slightly, then some light would strike one of the plates and be reflected. If a screen was set up about 3' from the exit of the light rays from the test unit, a sharp line was found to be superimposed upon the usual

light through the unit. This line approached coincidence with the boundary of light only when the plates approached being parallel with this parallel light. If the unit was twisted past the point of being parallel, then the same phenomena occurred although propagated from the opposite plate. In short, alignment at the point at which no reflected lines appeared on the screen was assurance of the parallel nature of both light and plates. Addition of heat, which refracted the light causing slightly non-parallel beams, caused no apparent effect on this procedure.

As already brought out, the measurement of the deflection of the refracted beam of light which grazes the heating surface (Beam AA in Figure 5) is necessary to find the temperature gradient. As can be seen by reference to Figure 4 or 5, the grazing beam starts from one side, crosses the horizontal centerline and appears on the screen. The distance deviated  $(Y_s)$  then is:

Y = Distance between inner boundaries on screen + 12D (23)

2

where, in this rait, D = 1.01/12 feet.

The wall temperature of the heated plate was constant across the aluminum plate but dropped off linearly through the transite-gasket strip to the window frame. As discussed previously, one-half of the thickness of the strip on either side is considered to be a part of the heating section. Equation 21, however, contains an absolute wall temperature term. It therefore becomes necessary to correct for the fact that over this section a different  $(\partial t/\partial y)_X$  and  $T_W$  exist.

Two assumptions are made:

1. That the average temperature (T,') of the transite-

rubber strip is the arithmetic average between  $T_{\mu}$  and the window frame temperature (taken as 100 F), or:

$$T_W^1 = \frac{T_W + 560 \, ^{\circ}R}{2}$$
 (24)

2. That the average temperature gradient through which the light passes in this region is one-half of the gradient from the aluminum plate.

Suppose that we now say that one unit length of aluminum plate under temperature  $T_y$  and gradient  $(\partial t/\partial y)_X$  gives a deviation  $(Y_s)$ . Under identical circumstances then, we find what deviation  $(Y_s^{-1})$  would occur for unit length of the transite-rubber strip. Solving Equation 21 for  $Y_s$  and setting up the ratio of deviations with the stated assumptions gives

$$Y_{e}^{'}/Y_{s} = (\frac{\partial t}{\partial y})_{x} (1/T_{s}^{'2}) / 2 (\frac{\partial t}{\partial y})_{x} (1/T_{s}^{'2})$$
 (25)

In the case of when t<sub>w</sub> = 500 °F, the ratio is 0.800. This means that one unit length of the transite-rubber insulation strip is equivalent to 0.800 units of the aluminum plate with respect to refracting the passing light. The effective heating length based on T<sub>w</sub> for this case is, therefore, the length of the aluminum plate plus 0.800 times the transite length (which is 18/16"). This gives a value of a<sub>h</sub> = 8.90". The accepted value for this unit (as was explained previously) is 8.56". To avoid complications, it was decided to multiply Equation 21 directly by the correction factor of the standard a<sub>h</sub> to the new a<sub>h</sub>. Such correction factors for t<sub>w</sub> = 500, 400, 300, 200, and 100 °F are, respectively, 0.958, 0.968, 0.978, 0.987, and 1.000.

(26)

The value of  $(\partial t/\partial y)_{XV}$  for any particular value of x is then calculated by use of Equation 21, remembering that:

- 1. Y is calculated by Equation 23 from the photographic record.
- 2. T, at x is obtained from a graph of Table 5.
- 3. The aforementioned correction factor is applied.
- 4. Barometric pressure is allowed for.

Use of these values gives the calculated values of  $(\partial t/\partial y)_x$  as tabulated in Table IX.

The total heat transferred to the air from this section is calculated precisely as described for the case of temperature gradients by traveling thermocouples. As before, use is made of Equations 19 and 20.

Values of  $Y_g$ , gradients, and  $q_V$  from these gradients are listed in Tables VII, IX, and X, respectively.

## Heat Transfer as Calculated by Average Inlet and Outlet Temperatures

The standard method of measuring the heat to a fluid is to obtain the heat input and subtract losses. Such a method was impractical in this case due to the unusual design of the apparatus as well as low heat pick-up by the air. In such case it was felt that more accurate information might be obtained by taking the average inlet and outlet temperatures. The method is:

$$q = Wc(t_1-t_2)$$

The flow rate ranged up to a maximum Reynolds number of 4900. Under these conditions the velocity profile at the start of the heated section was very closely parabolic (18). With the temperature profile also at the start of the heating section, it was possible to find the average temperature  $(t_1)$  at x = 0, based on the assumption that there was a two dimensional velocity and temperature field.

The average velocity is given by the equation:

$$u_{av} = W / S (\rho_0 T_0 / T_1)$$
 (27)

and the point velocity is given by

$$u = \frac{6}{p^2} u_{av.} (py-y^2)$$
 (28)

The point density is related to the main body density by the equation

$$\rho = \rho_0 T_0 / T \tag{29}$$

and the mass flow rate is given by

$$W = a \int_0^D u \rho dy' \qquad (30)$$

where D is in feet.

Equation 27 is substituted into Equation 28. Equations 28 and 29 are substituted into Equation 30. Solution for the average temperature  $(T_1)$  gives

$$1/T_1 = \frac{6}{D^3} \int_0^D (Dy'-y'^2) dy'/T$$
 (31)

This equation was solved by ploting T versus y at x = 0. Temperatures were then picked off at points which corresponded to values of y which would fit in Gauss's six-point integration formula (15). The entire equation was then numerically solved by use of Gauss's formula. Table I gives the inlet temperature profile. Table X gives  $T_1$ .

A similar principle was used to find the mean outlet temperature. At a distance of  $1/\mu^n$  below the end of the heating plate, a contraction was set into the duct. The form of this contraction which is effectively a narrow slit running the full width of the duct, can be noted by observing the top view of Figure 2. It is well known that a constant velocity exists in a stream passing through such contraction (19). Therefore, the same method of calculation used at x = 0 can be used at the contraction. Equations for this case are identical with the former except that  $u = u_{av}$ . Solution gives:

$$1/T_{\rm e} = \frac{1}{D'} \int_{0}^{D'} \frac{dy}{T}$$
 (32)

where D'; expressed in inches, equals the diameter of the contraction (0.410").

It is to be noted, however, that the contraction was light below the heated section. In order to obtain the heat transferred to the gas in the heated section for comparison with the other two methods of obtaining heat transfer, a correction factor must be applied.

It was assumed that this strip, below the heated section, was 50% effective, or that the amount of heat transferred from x = 0 to the contraction was equivalent

to the amount transferred if the heating plate had been 12-1/8" long. Therefore:

$$q_h = \frac{12.00}{12.12} W_0 (t_1 - t_c)$$
 (33)

The flow rate was metered by means of sharp edge orifices which had been calibrated with calibrated gasometer. Orifice coefficients were as expected. Calibration error was estimated to be 1%, but, due to slight variations in the input voltage to the blower, usage error was advanced to 2%.

The specific heat at constant pressure was taken as 0.240 plus .003 correction for humidity.

The values of q calculated from the mean temperature change are listed in Table X.

## Consideration of Data for Analysis

In geometrical configuration, the test unit is a narrow rectangular duct. Nevertheless, it cannot be considered to be a true heated duct, since only two of the sides are heated. In a case such as this, it can be assumed that the two parallel heated plates are a slice cut from the classical case of air flowing between two heated planes of infinite extent.

We will choose the breadth of the section cut from the infinite plates as equal to the heated breadth (a<sub>h</sub>) of the unit. Formerly, then, the cross sectional area was 9.75" x 1.01", now an imaginary piece has been taken

out of each end and the new area is 8.56" x 1.01". The former breadth of 9.75" was not fully heated at the extremes; the new heated breadth can, as was discussed previously, be considered to have the full plate temperature ty.

It remains then to correct for the fact that the average velocity in the removed area is much lower than in the center "core" area.

Semiquantative relationships (20) show that if the point of cut-off is specified, a relation exists between the velocity at the cut-off point and the velocity at a specific distance from the wall in the center of the duct. In this case, the velocity at the cut-off is approximately the same as at 0.17 D from the heated surface in the center of the duct. Since at the center of the duct, the velocity from the wall is closely parabolic, the average velocity flowing through the cut-off end section may be approximated by:

$$u_{av.} = \int_0^{.17D} 6 u_m (\frac{y'}{D} - \frac{y^2}{D^2}) dy' = 0.5 u_m$$

It will be assumed that the weight flow is proportional to the linear velocity. The "core" area is 88% of the old area. Therefore the weight rate in the "core" can be expressed by use of the area and velocity relationships mentioned. Then.

$$W_h = 0.88 W + \frac{0.12}{2} W$$
 (34)  
= 0.94 W  
 $G_h = \frac{0.94 W}{3}$  (35)

where 
$$S_h = a_h D = \frac{8.56 \times 1.01}{144} = 0.0601 \text{ sq.ft.}$$
 (36)

Note that the extremes of error for flow down this "core" are  $\frac{1}{2}$  6%. These extremes are: 1) no flow in the excluded cross section, and 2) uniform velocity over the entire cross section of the duct. Probable accuracy of flow down this "core" is  $\frac{1}{2}$  2% of the true flow.

For purposes of consistency, all future calculations concerning heat transfer coefficients will be based on Gh. This assumes that all of the heat goes into the amount of air expressed as Gh. Such is not the case as some mixing occurs. Error introduced in this assumption affects the value of the calculated heat transfer coefficient (hg) since it is based on the arithmetic average temperature rise between two points. However maximum error from this assumption proves to be 1.8% and decreases quickly as the flow rate increases.

## Range of Investigation

Flow rates of runs are identified by letters, thus:
Approximate Reynolds Number, 900 1800 2700 3600 4800
Identifying letter,

A B C D E

Wall temperatures are identified by numbers, thus:
Approximate Wall Temperature, 200 300 400 500
Identifying number, 1 2 3 4

If two runs were made at the same general conditions, they are differentiated by a letter "a" or "b" after the number.

All combinations of conditions involving the five letters and four numbers were made. One special run (x-4) had a Reynolds number of 1440.

#### RESULTS

## Comparison of the Three Methods

The optical method of determining temperature gradients in the air adjacent to the wall agrees very well with thermocouple measurements. Based on the total heat transfer from the heated section as calculated by temperature gradients, Equation 20, Q was found to agree with Q within an absolute error of 3.8% and an average error of 1.1%. Despite the good agreement, optical measurements were found to be more consistent.

The heat to the section as calculated from the air inlet and outlet mean temperatures, Equation 33, gave an absolute difference of 21.5% and an average of +7.0% from q. Results obtained from the inlet and outlet air temperatures were not consistent. For instance in runs C-4, D-4, and E-4, optical pictures showed the usual pattern for forced flow with no apparent buoyant effects; nevertheless, as the flow rate increased in these runs q, decreased. This is contrary to all previous evidence.

Due then to the greater consistency and more likely accuracy, it was decided to use  $q_{\psi} = q$  for all future calculations.

# Mechanism Analysis

Variation in the local heat transfer as the flow rate decreases (E to A) can be noted by reference to Figures 10 and 11. These plot variation in temperature gradients (which are proportional to q/A) versus x for a particular wall temperature (500 °F). The D and E runs follow the

expected variation in that q/A decreases approximately by  $(1/x)^{1/3}$  (note Figure 15). As the flow velocity decreased, however, a "hump" appeared in the curve. The exact description of this phenomena can be best illustrated by reference to Run X-4.

A plot of the approximate theoretical variation of the heat transfer coefficient with the actual local coefficient in Run X-4 is given in Figure 14. With the entering Reynolds number at 1440 the flow was essentially laminar. As the gas passed into the heated section, heat flowed from the wall into the gas in accordance with Equation 8. With the low flow rate, the gas near the wall became buoyant and its velocity became slower than isothermal flow calculations would indicate. This stagnation of flow near the wall caused a decrease of the heat transfer below what would be expected.

Before the gas near the wall flowed much farther, its density change was sufficient to cause upward flow at the wall. Such upward flow created a semi-turbulent condition. The heated layers near the wall are thrown into the core of the gas stream. This, therefore, effectively brought the core temperature much nearer to the wall and a sharper temperature drop occurred per unit distance from the wall. As can be seen, a sharp increase in the heat transfer resulted.

The semi-turbulent condition and rapid heat transfer rate raised the core temperature quickly. Since the buoyant effect depended upon the density difference between the core and the gas adjacent to the wall, a decrease in the velocity of the gas near the wall resulted. This stagnation again reduced the heat transfer. At some point then the temperature of the core had become close enough to that of the wall so that the flow shear again reverted the wall film to downward flow. Run A-4, Figure 10 shows the beginning of this condition.

Reference to Figure 9 shows the temperature profiles at different values of x in Run X-4. At  $x = 1^n$  and  $4^n$  it is obvious that laminar flow was still controlling the heat flow. By  $x = 7^n$ , it can be seen that the semi-turbulent condition caused by upward flow at the walls had greatly increased the core temperature and the temperature gradient at the wall. Further evidence of this phenomena can be noted by attention to Figure 8.

As discussed previously, Figure 8 shows thially the exact boundary of the heated film. Note that the upward flowing film seems to tear off into the main core. This variation of the film thickness causes fluctuations in the local heat transfer coefficient with time. Note the waviness of the outer boundary of light. This light had passed adjacent to the heated surface. Indentations indicate where the temperature gradient was momentarily steeper. Variations in gradient with time made it necessary to average a number of photographs; however, variation between views was not excessive as can be noted by observing Figure 7.

It is of interest to note that even under these turbulent conditions the gradient was approximately a straight line to  $y = .1^{\text{H}}$ . Maximum deviation (Run E-4) of initially grazing light was  $0.05^{\text{H}}$  from the heated surface when leaving the unit.

If the Runs A-1, A-2, A-3, and A-4 are examined they are found to increase in temperature and to have approximately equal Reynolds numbers. The buoyant counterflow is seen to become more apparent as the temperature increases. Increase in temperature or decrease in flow rate thus are, as expected, variables which increase the tendency for the upward flow.

### Comparison and Analysis

Norris and Streid<sup>(5)</sup> have collected and plotted some of the complex analytical solutions for heat transfer to a fluid flowing in steady state laminar flow. These equations assume constant physical properties and constant wall temperature. A plot of these equations is given in Figure 12. Coordinates are tabulated in Table XII. Heat transfer coefficients as expressed in these equations are defined by Equation 13.

Using  $q_v$  over the 12 inch long heated section (Table X), we found the temperature rise of the air flow  $G_h$  from  $t_1$  to  $t_2$ . Combining  $D_e$ , Equation 13, and 20, we obtained the average Nusselt number (notice that for infinite plates  $D_e = 2b$ ).

The data are plotted against the coordinates of Figure 12. The line for the average Nusselt number for flat ducts (infinite plates) from Figure 12 is also plotted on the same graph. These results are presented in Figure 13.

Since k does not vary much with air, the decrease of the function Ø is largely due to the drop of G in value. It is noticed then that as G decreases, the data fall under the theoretical curve. This could be caused by two effects:

- 1. The resulting slowing down of the film due to the increased buoyant effect on the slower fluid.
- 2. Emergence from the lower transition into the fully laminar region of flow. No matter which effect predominates, the data are no less than 25% under the theoretical equation.

As soon as the flow rate becomes low enough to cause a reversal of flow near the wall, the Nusselt number climbs again to values over the theoretical. However, when the buoyant forces are of the same order of magnitude as the forced flow forces (as the data are), the upward flow will again approach the theoretical.

Therfore in the range investigated, it can be said that the average Nusselt number will be within #25% of the values predicted by the plots of Figure 12.

In the case of small L/D ratios as say 1.5 in Run X-4. (Fig. 14) such statements may not be true; however such a small L/D would rarely be found.

In the range in which the buoyant force is much greater than the forced flow forces, it appears that the Nusselt number would approach values given by heat transfer to a cooler fluid in a vertical tube, the lower end of which is closed.

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## NOMENCLATURE

= surface area of that part of duct which transfers A heat (for a flat duct it includes both sides if both are transferring heat), sq ft = longest side in the perimeter of a duct, ft meated portion of a = shortest side in the perimeter of a duct, it C = 2a+2b = perimeter, ft = orifice discharge coefficient, dimensionless = specific heat. (at constant pressure), BTU/1b/oF D = diameter or distance between plates for a flat duct, ft = D for orifice flow meter Do = D for the pipe at the flow meter De = equivelent diameter = 4S/C, ft F = frictional force, lb force/sq ft/ft = W/S = weight velocity, lb/sq ft/hr G = G based on S<sub>h</sub>, lb/sq ft/hr Gh = conversion factor, 1b mass ft/lb force hr2 g<sub>c</sub> = acceleration due to gravity or centrifugal force g<sub>I.</sub> ft/hr2 h - heat transfer coefficient based on particular temperature differences indicated by subscript used with h, as defined by Equation 13, Bru/hr/sq ft/F = h on arithmetic-mean-temperature basis (see  $h_a$ Equation 13) hi = h on inlet-temperature-difference basis (see Equation 13)  $h_{L}$ = h on logarithmic-mean-temperature basis (see Equation 13) = h on local-temperature-difference basis (see h Equation 13)

kw = thermal conductivity of fluid at wall temperature;
BTU/ (hr) (sq ft) (°F)/(ft)

= distance from entrance of heated portion of duct, ft (unless otherwise stated)

L' = portion of traveling thermocouple wire exposed to
 radiation, ft

Lopt - optical length measured from center of heating rlate to screen, inches

Npr = cu/k = Prandtl number, dimensionless

 $N_{Re}$  = GD/ $\mu$  = Reynolds number, dimensionless

N<sub>Re</sub> = N<sub>Re</sub> through the orifice

 $N_{Re_1} = N_{Re}$  based on inlet temperature (t<sub>1</sub>)

N<sub>Nu</sub> = h<sub>a</sub> D/k, average Musselt number, dimensionless

P a = pressure drop, lb force/se ft/ft

p = absolute pressure, 1b force/sq ft, unless otherwise stated

P<sub>b</sub> = barometric pressure, cm water

Ph = barometric pressure, mm Hg

Pd = absolute pressure at the downstream flow mater pipe tap, cm water

Pu = absolute pressure at the upstream flow meter pipe tap, cm water

q = total heat transfer, based on a particular method of arriving at the result as indicated by the subscript used with q, BTU/hr

q based on temperature rise of the air through the
test unit (see Equation 33)

q<sub>t</sub> = q based on (at/ay)<sub>aT</sub> as calculated from thermocouple readings at fixed distances from the wall (see Equation 20)

```
= q based on (\dt/\dy)aV as calculated from visual
^{V}p
          measurements (see Equation 20)
q I
        = heat energy developed in unit volume and time,
          BTU/hr/cu ft
        = cross sectional area for fluid flow, sq ft
        = S for the area a,b, sq ft
        = absolute temperature designation of t, deg R
        = fluid temperature, deg F
        = traverse mean (mixing cup) temperature of the
          fluid, deg F
        = t<sub>m</sub> at entrance of heated portion of duct, (x=0),
tı
          (see Equation 31)
        = t<sub>m</sub> at any distance (x) down heated portion of
t_2
          duct
        = t_{in} at contraction (see Equation 32)
td
        = reference fluid temperature, or average temper-
to
          ature at the flow meter, deg F
        = wall temperature, deg F
        = t_w - (t_1 + t_2)/2, deg F
        = velocity, ft/hr
u
        = u average for the entire cross section of duct
\mathbf{u}_{\mathbf{m}}

    u in x direction

ux
u_v
        = u in y direction
        = u in z direction
\mathbf{u}_{\mathbf{z}}
111
        = total mass flow rate of flaid, lb/hr
W_{\mathbf{h}}
        - W through the "core" cross section (a,b) (see
          Equation 34)
        = axial distance from the entrance of heated
X
          portion of duct, inches
        = x in dimensions of feet
x'
Y
        = measured screen deviation of refracted light,
          inches (see Figure 5)
```

0

= shortest distance between the heated surface У and the duct axis and is measured from the wall, inches

= y in dimensions of feet y 1

= distance perpendicular to the duct axis and parallel to the heated surface, inches

= z in dimensions of feet

= k/pc, thermal diffusivity; sq ft/hr

= absorbtivity, dimensionless

= time, hr

= viscosity of fluid, (lb force)(hr)/(sq ft)

= density, lb/cu ft

= p at temperature to, lb/cu ft

(at) = air temperature gradient at the heated surface (y=0), deg F/ inch

 $(\frac{\partial t}{\partial y})_{\downarrow} = \frac{\partial t}{\partial y} \text{ at } x$ 

 $(\frac{\partial t}{\partial y})_{xT} = (\frac{\partial t}{\partial y})_{x}$  as determined from traveling thermscouple

 $(\frac{\partial t}{\partial y})_{xy} = (\frac{\partial t}{\partial y})_{x}$  as determined from optical measurements

 $(\frac{\partial t}{\partial y})_{c} = \int_{0}^{L} (\frac{\partial t}{\partial y})_{x} \frac{dx!}{L}, \text{ deg F/inch}$ 

 $\left(\frac{\partial t}{\partial y}\right)_{aT} = \left(\frac{\partial t}{\partial y}\right)_{a}$  as determined from traveling thermic couple

measurements

 $\left(\frac{\partial t}{\partial y}\right)_{aV} = \left(\frac{\partial t}{\partial y}\right)_{a}$  as determined from optical data

 $=\frac{\mathbf{c} \cdot \mathbf{D}^2}{\mathbf{k} \cdot \mathbf{r}}$ , dimensionless

#### APPENDIX A - SAMPLE CALCULATIONS

# 1. Calculation of Y<sub>s</sub>.

Using x = 3" from Run E-4 as an example, we find from the primary data that:

from Equation 22 then:

3

$$\beta = 1 + \frac{0.31}{0.144} \left( \frac{2.240}{553} \right)^2 \frac{(760)(955)}{756} = 1.0322$$

Substituting in Equation 21 and multiplying by the correction factor as indicated on page 29 gives:

$$(\frac{\text{at}}{\text{ay}})_{xV} = (0.958) \frac{(2.240)(955)^2(760)(1/12)}{(0.144)(1.0322)(766)(8.56/12)(563)}$$
  
= 2720 deg F/inch

# 2. Calculation of qy.

Calculation of the average value of  $(at/ay)_{xV}$  over the length L can be accomplished by graphical use of Equation 19.  $(at/ay)_{xV}$  is plotted versus x and either graphically integrated or specific points are taken which fit Gauss's numerical integration formula (15). Such an

integration for Run E-4 gives:

$$\left(\frac{\partial t}{\partial y}\right)_{aV}$$
 = 2552 deg F/inch

The heat flux to the air through the test unit is expressed in Equation 20 as:

$$q_V = 12k_W(\frac{\partial t}{\partial y})_{aV}$$

Substituting the above values gives:  $q_v = (12)(0.0248)(1.425)(2552) = 1042 BTU/hr$ 

# Calculation of Niu

A graphical plot of the temperature profile at the start of the heated portion of the duct (x=0) in conjunction with Equation 31 gives t<sub>1</sub>. This is accomplished either by graphical integration or use of Gauss's numerical integration. For Run E-4,  $t_1 = 107.1 \text{ deg F.}$ 

Solving for  $t_2$  in Equation 26 gives:  $t_2 = t_1 + \frac{q_V}{W_h C}$ 

$$t_2 = t_1 + \frac{q_V}{W_h C}$$

$$t_2 = 107.1 + \frac{1042}{(0.0237)(0.94)(3600)(0.243)} = 160.5$$

then,

0

$$\Delta t_a = 494.9 - \frac{160.5 + 107.1}{2} = 361.1 \text{ deg } F$$

Combining Equations 13 and 20 and multiplying both sides by De, we have:

$$N_{\text{Hu}_{a}} = \frac{h_{a}D_{e}}{k_{w}} = \frac{12(\frac{\text{dt}}{\text{dy}})_{\text{aV}}D_{e}}{\Delta t_{a}} = \frac{(12)(2552)(2.62/12)}{361.1}$$
$$= 13.72$$

TABLE II

CONTRACTION TEMPERATURE PROFILE

AT DISTANCE, x, = 12 1/4" FROM THE TOP

RUN		Distance f	rom Wall,	y, Inches	
NO.	•300	•350	•400	•450	•500
A-1	152.0	146.8	142.0	137.5	137.6
A-2	207.2	200.4	189.5	182.5	181.1
A-3	280.5	269.C	263.7	249.3	248.0
A-4	355.9	339.2	329.6	319.4	311.1
X-4	295.1	280.7	259.9	240.1	235.3
B-la	139.3	130.6	114.7	107.9	105.6
B-1b	146.4	137.0	123.1	112.5	111.6
B2a	170.2	158.5	148.4	133.1	127.7
B-2b	194.8	174.6	154.1	137.3	131.0
B-3	205.4	189.7	180.8	172.5	168.5
B-4	256.7	241.6	229.C	218.7	212.6
C-1a	132.3	120.6	109.7	101.0	101.5
C-1b	143.0	126.6	118.2	111.5	112.4
C-2a	159.7	140.9	121.0	108.5	107.9
C-2b	170.0	153.3	132.3	119.9	119.8
C-3a	206.4	180.9	155.3	137.3	129.5
C-3b	204.2	179.4	155.3	136.3	131.0
C-4	252.4	207.2	181.2	162.6	149.8
D-la	126.0	113.6	103.6	101.4	102.6
D-1b	136.0	124.1	116.5	112.9	113.1
D-2	162.2	138.9	119.7	110.6	110.
D-3	196.7	174.8	135.2	123.4	121.2
D-4	243.9	194.8	159.3	141.8	142.4
E-1	132.7	121.4	114.6	112.4	112.6
E-2	157.7	132.4	123.9	117.5	118.8
£1−3	176.8	145.5	126.8	118.8	121.1
E-4	212.4	166.3	136.1	127.6	127.

<sup>#</sup> All Temperatures are in OF

TABLE I

INLET TEMPERATURE PROPILE AT THE TOP, x = 0

		ഗ (	m	~	m	_		~	•		4	_,	œ	^		<u>.</u>	^	O>	ω		i.			٠.	, ,,			m	ے۔	•			
	200	83.5	ů.	666		69.1	• ·	-	-	=	103,4			ď	• (	ė.	4	လ	99	4	03.	ĵ.	0	, ; ;	3 8			8	S	104	Ö		
	400	83.4	86.	•	10.	87.5	•	•	•	•	103.3		94 .2			•	•	•	<b>50.4</b>	•		•	a	•	1 do		•	60	08		05.		
,	•300	85.1	94.	9	18	94.9	• •	-	•	-	103.9		95.0		•	•	•	•	95.9	•	•	9	9		200		3	60	80	03	103.1		
hes.	\$200	112.9	14.	57.	97.	127.7	•				07.	9	107.5			•	93		97.3		90				000	- 0	•	98	60	3	104.3		
, y, Inches	.150	116.3	ຜູ້	ີ	o	3 90 6	2	1	107.9	1	115.8	1	1		100	10%		110.5	1	113.7	116,3	1	0 001	3		2	117,47	070	60	.90	107.5		
from Wall,	.100	1	1	1	1	0.820	3.003	110.0	1	131.8		173.0	216.4	100			115.3	1	142.E	1	1	6.46	• 1		1000	•	1	1	1	-	1		
Distance fr	•075	135.3	79	56.	98			1	129.0	1	155.7	1	1			121.1		143.0	1	165.4	154.8		117 0	•		200	16%	13	26.	37.	145.1		
D1s	•050	149.1	88	81.	42.	2360	•	36.	40.	56.	8	39	293.5	00	99	32.	57.	52	.212.6	02.	33.	2	2 0	- 0	140°C	300	ρ	24.	47	65	201.8		
	•025	159.4	•	•		240 6	ů	52.	54.	926	66	94	333.7	1	-	48	83	86	255.5	33.	66	CK	) v	9 0	8 0 0 t 0	900	81	43.	85.	20	278.3	fn P	
	•0075	+	1	+	Ì		i	1	İ	215.2	1	305.4	377.8	и В	TOO.	1	209.6	1	284.7	1	1	148.0	•	3	1000 1000 1000	•		1		1	1	ires are	
	.005	171.2	36	8	366.9		3000	174.6	167.9		224.6				1	163.6	1	226.8	1	274 °C	342.1		2	C.LCT			328.1	161.8	223.4	267.3	347.7	Temperatures	
	NO.	A-1	C)	A-3	A-4		γ <u>-</u> 4	E-18	3-1b	C-C	B-2b	E. E.	) <del> </del>	•	-4	디	S	2		3	4	-	#	-+ (		2-7	70	, k	L C	(A)	B-4	* A]]	1
		I																															

TABLE III-a

GRADIENT TEMPERATURES, °F

Run	Distance from Wall			Distance	from	Top, x,	inches	
No.	I, inches	0	1	3	6	9	11	1134
A-1	0.005 0.025 0.050 0.075	171.2 159.4 149.1 135.3	199.5 188.4 179.6 166.6	205.0 196.9 185.4 177.2	207.0 198.0 187.7 177.2	203.9 192.7 179.2 167.4	200.9 192.9 181.8 172.3	196.1 190.3 180.3 173.8
A-2	0.005 0.025 0.050 0.075	236.3 213.6 188.1 179.3	273.9 254.7 234.6 210.2	282.7 269.8 255.1 244.3	282.0 260.8 240.5 215.9	284.7 271.5 253.3 237.7	281.0 268.5 256.8 242.6	273.1 265.5 255.4 246.4
<b>A-</b> 3	0.005 0.025 0.050 0.075	318.0 300.0 281.8 256.0	376.8 360.0 335.6 316.8	367.9 365.9 334.2 306.1	398.0 377.5 344.2 311.8	397.1 380.7 362.2 339.2	389.3 374.6 359.9 339.6	378.5 366.4 357.5 344.0
<b>A</b> -4	0.005 0.025 0.050 0.075	396.9 371.3 342.7 298.8	468.7 447.3 417.8 391.3	481.0 445.2 397.2 360.9	494.9 464.6 430.9 392.4	496.2 476.7 451.4 426.3	487.5 469.3 452.4 430.8	476.9 464.2 446.3 433.2
X-4	0.005 0.025 0.050 0.100	398.9 348.6 316.2 256.2	467.9 438.4 399.8 324.6	487.4 459.9 427.0 367.0	See Table IV	486.3 448.4 404.3 320.8	475.5 451.6 414.3 359.5	461.3 440.8 418.4 369.4
B-la	0.005 0.025 0.050 0.100	174.6 152.9 136.6 110.0	195.1 180.0 163.9 135.8	201.0 189.2 177.1 152.9	205.9 196.1 186.0 162.3	204.6 197.2 186.1 169.0	200.9 194.2 186.4 171.0	183.8 181.4 179.5 170.2
B <b>-1</b> 6	0.005 0.025 0.050 0.075	167.9 154.3 140.8 129.0	200.5 186.3 170.6 156.9	206.1 195.8 183.2 172.1	209.5 200.5 191.3 180.9	208.3 201.9 193.4 183.4	205.5 198.9 191.3 184.2	201.7 196.8 191.8 185.8
B-2a	0.0075 0.025 0.050 0.100	215.2 192.1 156.2 131.8	274.8 255.1 211.2 179.6	285.2 269.4 237.1 207.9	293.3 281.7 249.3 230.9	291.5 278.8 250.6 225.2	283.7 268.8 233.2 204.4	273.2 262.5 230.3 209.8
B-2b	0.005 0.025 0.050 0.075	224.6 199.0 180.8 155.7	283.4 261.7 236.1 211.9	295.5 278.9 260.4 239.0	303.5 288.7 272.2 254.1	302.2 290.3 275.1 259.6	295.2 283.9 271.5 255.6	286.7 277.5 265.6 251.9

TABLE III-b

GRADIENT TEMPERATURES, °F

Run	Distance from Wall		D	istance	from T	op, x,	inches	
No.	y, inches	0	1	3	6	9	11	113/4
B-3	0.0075	305.4	363.4	377.6	387.2	380.2	368.0	351.2
	0.025	276.4	337.4	357.0	368.9	357.4	342.9	331.6
	0.050	239.3	304.5	330.4	345.8	328.3	304.8	304.6
	0.100	173.0	242.9	281.5	292.6	266.9	248.0	255.5
B-4	0.0075 0.025 0.050 0.100	377.8 333.7 293.5 216.4	455.6 424.1 381.6	474.7 453.7 419.1	464.8 463.1 432.0	469.7 438.3 393.8	453.7 421.5 374.2	437.9 419. 377.
C-la	0.0075	153.5	188.8	194.6	199.0	198.4	194.6	189.0
	0.025	137.7	172.3	183.7	188.4	188.8	186.8	186.0
	0.050	122.7	153.9	169.8	176.0	179.2	179.5	180.0
	0.100	100.7	117.6	139.6	147.3	151.7	154.2	160.0
C-1b	0.005	163.6	195.7	202.9	207.3	206.9	203.6	200.
	0.025	148.4	178.9	190.3	197.3	197.3	196.1	195.
	0.050	132.5	161.5	176.0	184.6	188.3	186.5	188.
	0.075	121.1	144.9	161.6	173.0	161.0	176.6	179.
C-2a	0.0075	209.6	270.8	283.4	291.0	286.8	282.4	277.
	0.025	182.7	244:.9	265.0	273.5	274.4	268.7	267.
	0.050	157.6	215.0	237.0	252.2	253.7	252.2	250.
	0.100	115.3	153.1	191.9	204.0	206.8	208.3	214.
C-2b	0.005	226.8	280.6	294.1	300.8	299.2	291.9	284.
	0.025	192.2	252.0	271.9	282.0	284.4	278.9	274.
	0.050	162.9	218.8	245.4	259.3	264.9	261.4	259.
	0.075	143.0	190.9	221.2	236.8	243.1	239.6	245.
C-3a	0.0075	284.7	358.0	373.6	382.8	378.5	367.7	345.
	0.025	255.5	327.1	348.6	363.2	357.7	347.9	337.
	0.050	212.6	284.2	312.4	325.1	297.7	325.2	314.
	0.100	142.8	201.4	248.2	263.8	269.6	263.9	265.
C-3b	0.005	274.0	361.5	383.1	393.9	390.6	380.7	366.
	0.025	233.8	321.0	350.9	367.9	367.0	359.0	350.
	0.050	202.0	281.2	322.1	340.0	343.4	336.1	329.
	0.075	165.4	242.0	287.9	308.2	309.7	306.1	306.
C-4	0.005	342.1	453.9	480.4	491.9	487.1	470.3	454.
	0.025	299.5	402.8	440.9	460.5	456.8	445.3	433.
	0.050	233.0	345.5	396.3	419.9	423.3	406.4	397.
	0.075	194.8	298.1	359.3	383.2	388.9	370.1	368.

TABLE III-c

GRADIENT TEMPERATURES, °F

Run	Distance from Wall		Di	stance	from To	p, x, in	ches	
No.	y, inches	0	1	3	6	9	11	1.13/4
D-la	0.0075	148.2	187.4	194.3	198.4	199.1	194.7	193.0
	0.025	132.5	168.8	161.5	186.8	190.7	186.2	187.
	0.050	115.1	146.9	161.8	171.6	176.3	173.5	178.0
	0.100	97.9	110.4	169.1	137.9	144.8	145.3	153.0
D-1b	0.005 0.025 0.050 0.075	157.3 145.6 127.3 117.9	191.3 174.8 154.7 136.3	199.3 186.1 169.6 153.2	203.8 192.9 178.8 163.5	203.7 193.2 182.1 168.9	199.7 191.9 181.8 168.6	196. 190. 182.
D-2	0.0075	198.0	267.3	280.3	289.5	287.8	281.4	278.
	0.025	166.9	237.0	258.1	269.5	271.5	266.2	266.
	0.050	140.3	201.0	228.1	245.9	250.2	248.5	249.
	0.100	106.7	133.6	168.4	186.7	195.9	194.0	202.
D-3	0.0075	297.0	356.7	375.6	381.4	380.5	376.6	352.
	0.025	239.1	319.9	346.3	357.1	358.3	347.6	338.
	0.050	192.5	271.3	307.2	321.2	323.4	317.4	310.
	0.100	122.7	169.4	218.0	242.2	247.3	242.4	257.
D-4	0.005	328.1	1449.2	475.5	487.6	483.0	469.6	452.1
	0.025	281.1	398.8	436.7	455.5	452.4	440.6	430.9
	0.050	218.7	339.4	381.6	413.5	412.8	407.7	404.9
	0.075	167.0	264.8	327.5	354.2	361.6	364.3	368.
E-1	0.005	161.8	200.7	209.2	212.3	210.4	206.5	204.
	0.025	143.1	180.4	192.2	197.0	197.5	196.0	196.
	0.050	124.1	152.6	170.6	177.9	181.0	180.9	184.
	0.075	113.0	130.6	148.0	158.6	161.7	164.2	170.
E-2	0.005	223.4	283.5	297.6	300.9	299.4	292.7	286.8
	0.025	185.6	248.8	268.7	277.9	279.1	274.8	273.9
	0.050	147.3	201.9	231.3	243.8	249.0	247.9	252.1
	0.075	126.4	161.3	192.9	208.3	210.8	214.3	220.1
E-3	0.005	267.3	361.6	380.2	387.9	381.3	372.8	361.6
	0.025	220.7	311.6	341.1	356.4	353.3	348.6	243.6
	0.050	165.6	250.0	288.9	312.6	315.2	313.0	315.5
	0.075	131.4	189.7	234.9	259.0	265.4	265.3	278.6
E-4	0.005	347.7	460.7	483.0	493.5	484.1	470.6	454.1
	0.025	278.3	397.0	434.1	451.9	444.3	436.0	429.7
	0.050	201.8	317.6	365.2	394.7	394.6	390.9	396.1
	0.075	145.1	223.1	291.6	317.5	333.0	334.0	345.8

TABLE IV

THMPERATURE PROFILES RUN x-4

Distance From		D	istance	from t	he Top,	x, Inc	hes		
Wall, y Inches	0	1	3	4	5	7	9	11	11 3/4
•005	398.9	467.9	487.4	489.5	490.9	491.2	486.3	475.5	461.3
•C25	348.6	438.4	459.9	466.5	461.3	446.0	448.4	451.6	440.8
•050	316.2	399.8	427.0	424.6	425.3	398.5	404.3	414.3	418.4
•100	256.2	324.6	367.0	367.7	352.1	315.3	320.8	359.5	369.4
•150	179.8	247.2	302.4	298.8	293.4	261.3	280.7	300.6	328.9
.200	127.7	175.7	251.0	256.6	256.6	236.0	247.2	273.7	292.3
•300	94.9	100.5	152.4	184.1	204.1	213.4	218.8	246.1	264.1
•400	87.5	91.9	107.8	120.4	153.7	191.7	211.1	223.5	242.4
•500	89.1	90.3	108.6	111.4	128.1	183.0	211.9	221.6	233.8

<sup>\*</sup> All Temperatures are in oF

TABLE V
WALL TEMPERATURES

							_
Run No.				Top, x,		_	-
110.	1	3	5	7	9	11	_
A-1 A-2	203.1	207.3	209.7 293.6	210.9	209.7	206.0 286.9	
A-3 A-4	384.5 480.1	396.3 496.2	402.7 505.2	406.3	404.0 506.3	394.6 493.6	
X-14	477.6	494.3	502.2	504.9	500.3	485.2	
B-1a B-1b B-2a B-2b B-3 B-4	198.2 206.3 289.3 295.7 378.5 475.3	202.2 210.3 296.8 303.4 389.5 490.9	204.5 212.7 300.6 307.8 394.9 498.2	205.9 214.0 302.7 310.1 396.7 500.6	204.7 212.9 300.5 308.0 392.8 495.1	200.6 209.1 293.0 300.8 380.8 479.1	
C-la C-lb C-2a C-2b C-3a C-3b C-4	196.6 204.4 286.7 291.6 380.2 384.8 478.7	200.5 208.6 293.9 299.2 391.5 397.3 495.6	202.6 211.1 297.8 303.5 397.3 403.9 504.6	203.9 212.5 299.6 305.6 399.7 406.9 508.1	202.9 211.3 297.3 303.2 395.5 403.4 502.9	198.9 207.7 289.3 295.6 384.0 391.7 486.7	
D-1a D-1b D-2 D-3 D-4	198.0 200.7 288.0 380.0 477.6	202.3 204.8 295.6 391.4 494.6	204.8 207.3 299.7 397.1 503.6	206.2 208.5 301.8 399.9 507.3	205.1 207.6 299.5 396.2 502.2	200.8 203.8 291.3 383.8 486.0	
E-1 E-2 E-3 E-4	208.2 296.2 380.1 477.2	212.7 304.4 392.8 495.0	215.6 309.0 399.4 504.2	217.2 311.2 402.7 508.0	216.2 308.8 398.9 502.3	211.8 300.4 386.4 484.7	

<sup>#</sup> All temperatures are in °F.

TABLE VI

Run No.	Orifice Number	tg.Av.	P <sub>u</sub> - P <sub>d</sub>	Pd - Pb	Pb
A-1 A-2 A-3 A-4	1 1 1 1	103.0 103.1 111.4 111.5	24.8 25.6 25.5 25.3	0 0 0	1037 1037 1033 1028
X-4	1	105.4	60.8	0	1031
B-1a B-1b B-2a B-2b B-3 E-4	2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	115.8 118.6 110.0 121.1 107.6 111.3	16.3 16.0 1 <b>5.2</b> 16.0 15.5	0 0 0 0 0 0	1040 1031 1033 1036 1032 1031
C-la C-lb C-2a C-2b C-3a C-3b C-4	2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	114.8 125.0 110.8 122.8 115.7 121.0 116.2	35.3 36.3 35.3 36.2 36.7 35.9 36.3	1 1 1 1 1	1038 1031 1040 1039 1033 1041
D-1a D-1b D-2 D-3 D-4	2 2 2 2 2 2	117.0 126.1 116.2 114.7 122.2	63.5 64.3 65.1 64.5 64.7	2 2 2 2 2	1033 1031 1031 1030 1028
E-1 E-2 E-3 E-4	3 3 3 3	125.6 125.2 117.8 115.5	13.2 13.5 13.5	10 10 10 10	1032 1029 1039 1040

TABLE VII A

# OPTICAL DATA

Run No.	L <sub>opt</sub> Inches	Set*	Film Numbers	Films Used to Evaluate Ys
A-1	663	0-512	109-114	109-113
A-2	663	G-512	115-118	115-118
A-3	663	G-513	119-122	119-122
A-4	663	G-513	123-126	123,124,126
X-4	663	0-492	87-100	88,91-93,100
B-la	664	G-405	15-18	16, 18
B-15	663	G-587	161-165	163,165
B-2a	664	G-405	31-35	32, 34
B-2b	663	G-589	175-178	176,177
B-3	664	G-454	53-56	53-56
B-4	563	G-454	65-68	65-67
C-la	6614	0-1105	23-26	24-26
C-1b	663	G-588	166-170	167,168
C-2a	6614	G-405	36-40	37-40
C-2b	663	G-589	179-184	181,183
C-3a	664	G-454	57-60	58,59 190,192
C-3b	663	G-590	189-192	190,192
C-4	563	G-586	150-154	152,153
D-la	664	0-405	27-30	28-30
D-1b	663	G-588	171-174	172,174
D-2	664	G-405	47-52	49,50
D-3	563	0-454	61-64	62,63
D-4	563	G-587	155-160	157,160
E-1	663	G-513	127-130	127,130
E-2	663	G-513	131-137	133,136
E-3	563	G-516	138-145	141,145
E-4	563	G-586	146-149	147,149

Denotes file number of the film in the Photographic Department, University of Delaware, Newark, Delaware

TABLE VII-B

EVALUATION OF LIGHT BEAM DISPLACEMENT, Y

	12		ı	•	•	ı	•	0,5,0	•		•	1	ı		0.540	1 (	000.0	ı	ı	• 1		0.540	•		•	ı	ı	ı	•	•
	11 3/4	1	,0	Ö	0 0 0 0 0 0	•	•	•	•	•	•	,		,	•	•	•		11	700 100 100 100 100 100 100 100 100 100	•	•	•	•	•	•	•	•	1.255	•
	1172	9	. 0	0	0.840	•	ů	6	v	100	10	0	1.720	. 1	1	•	, a	500	2,0	1. 20. 70. 70.	1	1 7	5.4	9 5	10.	.18	.97	3	1.355	#
	11	5	) Q		0.0 10,00 10	•	7		.55	S	Ġ.	.91	1.850	' <b>(</b>	0 660	3	1 6	, c	- L	1.090	•		•	•	•			•	1.40	•
	10	9	2 0	•	0 0 0 0 0 0 0	•	o	7	·v	٦,	-	જ	œ	С	. [		40	, ר	•	40	С		- c	י ני		เป	ं	N.	1.00 to 1.00 t	j
	6	97	-	7	1.005 0.080	•	2.005		.61	0	. 93	.31	Ŋ			- 1	5	7	14	1.060	f	ξ Σ	, 2	, , , ,	7	.31	17	5,	4. 6.7 7.0 7.0 7.0	8
	8	7	• - u	i c	1,000	•	'n		9.	6	ξĎ	4	U.	C	00	,	1 -	• -		1.070	C	a c	, ה		•	.,	S.	0	0,4	٥
Inches	7	(1)	- 8	) L	1.190	t r	77.		69.	0.954	.90	ە. كى	ं	•	0.860		7	7	10	1.120		יס י	/α	-	1.	.43	.26	5.	1.745	v •
top, x,	0	.67	1,6	י ל	1.620	1	9	.86	.73	96.	34	0,	96.	.18	91	13	17	7	10	in	3	00	ট	1-	1-	07.	<u> </u>	<del>2</del>	ם מלט סקט סקט	S
ce from	75	.56	3.	70	1.775	n n	,	ı	77	1.049	7	•02	.93		0.945		. 32	13	6	1.280	1	·	ò	J.	, U	•	<u>ښ</u> (	<u>٠</u> ٥	1.975	•
Disten	4	.61	.18	76	1.885		•	76.	34	11	3;	11.	.93	.13	0.0	.62	. 39	in.	2	1.390	35	1	.73	5	7	5 .	177	1 C	90	•
	3	.61	.92	617	1.585	0		<u>.</u>	.91	22	17.	7	96.	ਹੌਂ.	80.	.73	7,	69.	.71	1.505	.47	8	9	78	76	•	200	700	5.5	1
	2	.63	.81		1.370	C	•	7	٠,	7	٠,١	٠	0		iQ.	0	7	0	C	1.760	9	~	0	0	O	,	0,1	Un	2, 5, 5, 5, 5, 5, 5, 5, 5, 5, 5, 5, 5, 5,	•
	1	•	•	•	1.095		•	•	•	•	•	•	•		•	•	•		•	2.15	O.	N	'n	'n	-	<b>†</b>	0	, <	000	•
	1/2	σ,	4	0	1.125	v	) ,	တ္ .	= 1	ન્ લ	ر د	٦!		6		ထ	'n	lω	0	2.57	7	ď	ක්	Ç	α	•	<u>ب</u> .	Į.	10	•
	3/16	c)	4	ĊŲ	1.320	2.055	)	• 1		2002	ئ در	60	8		2.065		0		-	3,22	,	1	ائی ر	10	·Л	Ů.	٥٠	์ เ	7.00°C	•
	0	Ň	.9	ည်	ľŪ	2.715	. 1	2.120	٠,	N C	٠ د	0	•	0	₹.	0	7	-	45	4.22	4	2.770	9	N	1	2	010	3,5	6,207	
Run	No.				A-4	X-h	T i	B-Ia	1	V	i		1			1	•		1			- 1	4	1			1	1	1 E	

\* Displacements are in inches.

TABLE VIII

TEMPERATURE GRADIENT AT THE WALL, (At ) at )

OF /INCH THERMOCOUPLE DATA

RUN	<del></del>		Distan	ce from	the Top.	x. Inch	93	
NO.	0	1	3	6	9	11	11 3/4	12
A-1	512	473	396	422	552	393	320	
A-2	1264	805	570	840	583	492	327	
A-3	878	861	858	1192	804	<b>6</b> 88	477	
A-4	1313	903	1758	1468	1005	814	627	****
X-4	3280	1506	1350		1773	1202	951	
B-la	1274	655	529	460	431	306		132
B-1b	742	678	444	432	338	298	222	
B-2a	1320	1124	833	710	700	845	676	
B <b>-26</b>	1€08	1044	808	700	604	564	<b>46</b> 8	
B-3	T9.15	1363	1168	1015	1225	1408	1158	
B-4	2874	1768	1252	1228	1790	1830	1320	
C-la	1144	733	596	558	506	440	97	
C-1b	666	818	<b>65</b> 8	548	496	396	304	
C-2a	1768	1235	1084	940	825	780	666	
C-2b	2016	1382	1144	912	758	680	564	
C-3a	1700	1750	1445	1280	1168	1113	925	
<b>C-</b> 3b	2050	1776	1.428	1210	1080	1035	820	-
C-4	2522	2288	1844	<b>1</b> 548,	1422	1452	1236	
D-la	1180	1054	722	<b>6</b> 56	565	493	324	
D-16	<b>6</b> 66	824	664	542	496	<b>3</b> 88	310	disense disens
D-2	2150	1522	1145	1147	914	882	797	
D-3	3794	2015	1700	1420	1332	1176	1043	
D-4	2414	2518	2134	1654	1666	1358	1068	
E-1	1060	1014	870	756	660	5 <b>6</b> 8	438	<del> </del>
B-2	1988	1750	1486	1364	1182	1038	766	Contract .
H-3.	2410	2440	2124	1676	1548	1402	1118	
P-4	3968	3170	2680	2208	1480	1462	1224	

<sup>\*</sup> All Temperatures are in OF.

AL PLACE

ř

TEMPERATURE GRADIENT AT THE MALL, ( &t.) , OF INCH. OPTICAL DATA

		12		281	285 639	280	
	: !	503 523 523 709	1343	4 7 0 0 0 0 0	401 302 642 552 805 1459	4.60 329 745 1238	490 861 1212 1631
	,	51 1/2 518 537 715 715	1375	2.84 8.89 6.39 2.590 2.04.5	323 602 855 865 1335	360 775 1 <b>23</b> 7 1423	521 919 1313 1720
		548 563 735	2	297 874 590 1560 2210	355 630 898 885 1336	382 803 1261 1525	561 1000 1410 1778
	<u>.</u>	540 642 828 917		376 306 779 550 1343 2220	425 389 789 679 934 1315	530 410 872 1302 1568	589 1065 1479 1917
	o	520 765 931 1067	2120	337 690 559 1114	416 717 975 1008 1349	445 912 1572 1661	626 1113 1561 2005
inches		423 867 1122 1330	2350	406 553 663 972 1573	475 869 759 1028 1370	576 476 956 1424 1747	666 1170 1680 2080
Top, x,		360 932 1360 1597	2250	377 630 904 1326	215 1079 1134 1433	509 1017 1470 1518	690 1230 1757 2160
from the		360 985 1518 1750	1610	452 401 677 661 899 1225	524 493 971 857 1157 1211	627 538 1059 1512 1862	717 1293 1852 2310
Distance	ເວ	299 899 1553 1915	1360	419 722 689 920 1174	510 905 1220 1290 1622	541 1127 1556 1896	746 1368 1940 2410
10	4	329 734 1516 2005	1242	489 457 751 745 943	594 1083 1083 951 1386 1740	711 600 1177 1662 2010	785 1472 2060 2520
	ы	325 615 1280 1731	1080	525 489 829 803 1087 1203	644 1157 1030 1426 1969	765 640 1260 1753 2180	832 1570 2235 2720
	2	335 536 . 979 1436	1117	574 555 946 933 1161	714 648 1277 1140 1584 1612	853 719 1394 1964 2380	905 1718- 2370 2980
	7	416 637 797 1128	1258	696 663 1157 1130 1420 1729	842 770 1520 1413 1917 2015	1020 817 1638 2430 2850	1067 1972 2820 3500
	1/2	513 717 964 1127	1538	831 769 1392 1372 1691 2050	1004 907 1346 1658 2305 2340	1225 969 1842 2850 3260	1250 2255 3190 3960
	3/16	646 392 1048 1430	2030	905 1730 1730 2100 2660	1080 1892 2940 2910 3610	1214 2100 3480 3890	1527 2630 3720 5150
	0	821 1216 1475 2010	2690	1079 1032 2030 1968 2790	1820 1858 2420 2180 3560 3500 4510	1570 1407 8850 3980 4840	2080 3260 4640 5860
RUN NO.	4.7	4444 40004	¥.	8 10 10 8 8 8 11 11 1 1 1 1 1 1 1 1 1 1	4848844 484884	40444 41444	<b>प्रकृ</b> ष्टि स् एक्ष्म्

\* All Temperatures in OF.

CALCULATED DATA DETERMINATION OF 9h, 9T, 9V, NRO1, Nug, \$

	191	94 76 76 76 76 76 76	111	194 186 170 152 141	0.444.499 0.874.499 0.874.4990 0.874.4900 0.	382 380 3044 280 280	494 441 405 371
	<sup>Ñ</sup> Re <sub>1</sub>	930 937 890 866	1440	1870 1800 1830 1820 1820 1820	2780 2710 2770 2770 2770 2720 2730	3700 3720 3680 3610	7,000 1,750 1,750 1,870 1,870
	<sup>g</sup> η 15/m//89 ft	250 251 252 252 243	1,00	500 500 500 500 500 500 500 500 500 500	747 7448 7450 7450 7450 7450 7450	1002 998 101 <b>3</b> 1009 1008	1312 1312 1329 1334
	N <sub>Nu</sub> g	8.77 9.73 10.87 10.38	10.48	10.14 9.05 9.23 9.43 9.67	11.88 11.37 10.63 9.70 10.14	12.53 12.53 11.558	15.84 15.47 14.91
ಥ	Δt op	96.8 153.8 208.8 274.4	320.0	96.7 182.4 177.0 253.3 333.4	97.9 181.9 176.1 266.1 351.6	97.7 89.7 18c.6 268.0 350.1	97.7 181.9 267.1 361.1
T	t2-t1 % (F=1')	35.6 68.6 118.0 163.8	119.9	20.5 26.3 26.3 26.3 7.9	44644409 6444999999999999999999999999999	12.2 26.6 43.4 57.8	4868 8868 9404
	q <sup>p</sup> B'īU/ar	130 255 434 596	200	136 290 265 672 672	1148 363 363 713 733	216 177 394 639 851	240 1756 1042
	(at/ay ky %/1nch	420 742 1123 1410	1555	485 834 834 760 1171 1590	527 1052 1052 1279 1320 1726	697 571 1137 1669 2004	766 1393 1971 2552
	°t Bru∕hr	143 235 377 525	655	150 136 263 263 641	178 339 731 7310 7310	216 177 402 617 820	245 1495 724 986
	(3t/3y) <sub>k T</sub> °F/Inch	461 684 976 1242	1547	1232 1732 1732 1732	572 577 1008 970 1384 1312	6927 11177 11607 1932	794 1419 1687 2329
	ж ж v	0.0182 0.0202 0.0227 0.0249	0.0246	0.0182 0.0203 0.0205 0.0225 0.0246	0.0180 0.0182 0.0204 0.0226 0.0228 0.0228	0.0181 0.0181 0.0203 0.0226 0.0248	0.0183 0.0205 0.0226 0.0246
	0.00 €t 13.00 €	207.6 290.1 397.5 498.1	493.7	202.1 210.8 297.0 303.9 388.5 489.5	200.6 299.2 299.5 391.3 495.7	2002 8 2002 8 2003 8 2000 8 2000 8 2000 8 2000 8 2000 8 2000 8 2000 8 2000 8 20000 8 2000 8 2000 8 2000 8 2000 8 2000 8 2000 8 2000 8 2000 8 20000 8 2000 8 2000 8 2000 8 2000 8 2000 8 2000 8 2000 8 2000 8 20000 8 2000 8 2000 8 2000 8 2000 8 2000 8 2000 8 2000 8 2000 8 20000 8 2000 8 2000 8 2000 8 2000 8 2000 8 2000 8 2000 8 2000 8 20000 8 2000 8 2000 8 2000 8 2000 8 2000 8 2000 8 2000 8 2000 8 2000	213.5 304.8 393.1 494.9
	<sup>4</sup> h B⊺U∕hr	186 355 497 718	116	174 157 390 359 597 919	1176 3377 6478 677 777	158 144 358 704 821	175 329 546 820
	<b>₩</b> 6	161 1935 26035 329 4	262.4	121.3	1111 120 136 136 136 136 137 137 137 137 137 137 137 137 137 137	107.8 118.9 124.9 146.6 169.1	126.5
	는 Ct	93.0 102.0 129.7 141.8	113.8	103.55 103.33 103.33	96.0 107.7 95.8 108.7 109.9	97.5 109.5 101.9 116.0	109.5 110.6.5 106.5
	1b/ 80c	0.00444 0.00451 0.00447 0.00443	0.00710	0.00901 0.00874 0.00875 0.00890 0.00883 0.00883	0.01326 0.01328 0.01330 0.01332 0.01330 0.01330	0.01779 0.01773 0.01800 0.01792 0.01790	0.0233 0.0233 0.0236 0.0237
	Run No.	4 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 -	オーズ	B-13 B-28 B-20 B-3	20000000000000000000000000000000000000	D-18 D-2 D-4	40 64 

TABLE XI

VARIATION OF LOCAL NUSSELT NUMBER WITH LENGTH

Run No.	L Inches	t <sub>2</sub>	t <sub>w</sub> -t <sub>2</sub> °F	(at/ay) °F/inch	h <sub>x</sub> D <sub>e</sub> Experimen	
X-4	0 1/2 12345678 90 112	113.8 118.6 123.1 130.8 137.0 144.3 152.6 163.9 176.7 190.8 204.0 216.1 226.0 234.3	348.2 352.0 354.5 356.4 357.3 354.7 349.6 340.3 328.2 313.0 296.3 277.7 259.2 240.7	2690 1538 1258 1117 1080 1242 1665 1910 2250 2350 2120 1783 1475 1310	15.31 8.83 7.19 6.34 5.10 7.07 9.62 11.31 13.84 15.17 14.46 12.99 11.50 10.99	18.07 14.17 11.38 9.92 9.04 8.46 7.87 7.49 7.12 6.86 6.64 6.41 6.25
E-4	0 1/2 1 2 3 4 56 7 8 9 10 11	107.1 111.0 114.5 120.6 125.5 130.3 134.9 139.1 143.1 146.9 150.6 154.2 157.5	356.9 360.2 362.7 366.6 369.5 369.3 368.1 364.9 360.1 351.7 340.9 327.2 309.5	5860 3960 3500 2980 2720 2520 2410 2310 2160 2080	33.31 22.22 19.51 16.44 14.89 13.78 13.19 12.67 11.98 11.66 11.51 11.35 10.99 10.18	30.68 21.39 16.97 14.82 13.49 12.48 11.77 11.19 10.69 10.28 9.93 9.61

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TABLE XII

# HEAT-TRANSFER RELATIONS

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# FOR PARABOLIC VELOCITY DISTRIBUTION

# AND CONSTANT WALL TEMPERATURE

	Roun	d Ducts		F	lat Ducts	
$\varphi' = \frac{cGD^2}{V}$	h <sub>1</sub> D	h <sub>a</sub> ⊃	$^{\mathrm{h}}\mathrm{L}^{\mathrm{D}}$	h <sub>1</sub> D	$h_{\mathbf{a}}D_{\mathbf{b}}$	h_D Le
$\varphi = \frac{kL}{kL}$	k	k	k	k	k	k
T	0.25	0.50	3.68	0.25	0.50	7.60
I 2 3 4 5 6	0.50	0.99	3.76	0.50	1.00	7.50
3	0.75	1.48	3.81	0.75	1.50	7.60
4	0.98	1.92	3.86	1.00	2.00	7.60
5.	1.20	2.29	3.91	1.24	2.48	7.62
6	1.39	2.60	3.96	1.49	2.95	7.65
	1.57	2.86	4.01	1.73	3.42	7.69
8 9	1.74	3.07	4.06	1.96	3.85	7.74
	1.89	3.25	4.11	2.18	4.23	7.80
10	2.03	3.41	4.16	2.39	4.58	7.86
12	2 <b>.27</b>	<b>3.6</b> 6	4.26	2.78	5.18	7.92
15	2.60	3.95	4.41	3.30	5.89	7.98
20	3.05	4.38	4.70	4.00	6.67	8.05
25	3.43	4.72	4.97	4.55	7.16	8.15
30	3.76	5,02	5.22	5.00	7.50	8.24
40	4.33	5.52	5.67	5.74	8.04	8.52
60	5.22	6.32	6.48	6.73	8.67	8 <b>.93</b>
	6.23	7.24	7.30	<b>7.</b> •87	9.54	9.67
130	7.27	8.18	8 <b>.23</b>	8.97	10.4	10.5
200	8.63	9.45	9.45	10.4	11.6	11.6
<b>3</b> 00	10.1	10.8	10.8	12.0	13.1	13.1
400	11.2	11.9	11.9	13.4	14.4	14.4
600	13.0	13.6	13.6	15.4	16.2	16.2
1000	15.6	16.1	16.1	16.8	19.5	19.5
5000	19.9	20.3	20.3	23.3	23.9	23.9
3000	55.9	23.3	23.3	20.4	26.9	26.9
4000	25.3	25.6	25.6	28.9	29.3	29.3
6000	29.0	29.3	29.3	33.1	33.5	33.5
10000	34.6	<i>34</i> • 8	34.8	39.6	39.9	39.9
20000	43.6	43.8	43.8	50.0	50.2	50.2
30000	50.0	5C.2	50.2	57.0	57.2	57.2
40000	55.1	55.2	55.2	62.6	62.8	<b>62.</b> 8

TABLE X111
THERMOCOUPLE CALIBRATION

ù					
	Iron-Co	nstantan	Copper-Constanta		
Temp.	Average Deviation from Standard	Maximum Deviation from Average Deviation	Average Deviation from Standard	Maximum Deviation from Average Deviation	
°F	٥F	°F	°F	٩°	
76.8	-0.5	0.36	-0.1	0.56	
105.2	-1.0	0.58	-0.1	0.53	
124.6	-0.9	0.53	0.1	0.54	
147.4	-1.3	0.58	0.0	0.62	
168.2	-1.6	0.56	0.1	0.70	
190.7	-2.2	0.61	0.1	0.70	
212.3	-2.2	0.64	0.1	0.70	
235.4	-2.4	0.68	0.2	0.70	
254.0	-2.5	0.78	0.1	0.78	
274.9	-2.8	0.81	0.3	0.86	
293.6	-3.1	0.89	0.5	0.86	
313.6	-3.5	0.92	0.5	0.89	
333.2	-3.3	0.94	0.6	0.91	
355.5	-3.7		0.8		
375.7	-3.5				

0

TABLE XIV

CRIFICE CALIBRATION

Orifice	D <sub>o</sub> ft.	N <sub>Re</sub> o	c <sub>o</sub>	
1	0.02475	8.200 11,590 15,220 18,100 22,060 25,900 30,150 33,100 36,150	0.621 0.613 0.607 0.614 0.605 0.606 0.605 0.603	
2	0.03935	18,700 23,800 29,550 34,130 40,100 45,400 51,650 55,150	0.613 0.609 0.606 0.601 0.604 0.604 0.603	
3	0.0656	30,660 40,900 49,200 59,500 69,400	0.625 0.628 0.625 0.625 0.625	

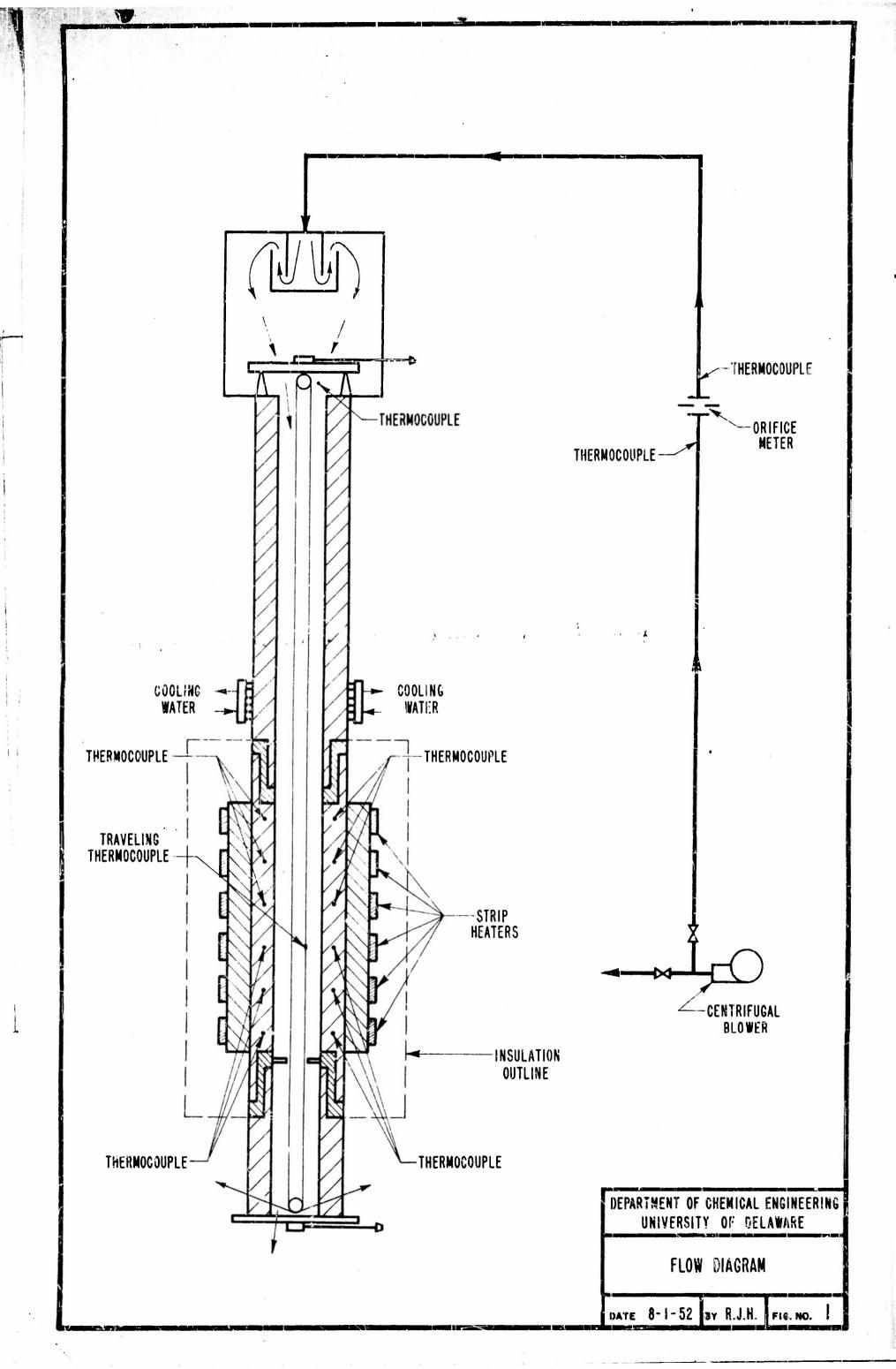
 $D_p = 0.1600 \text{ ft.}$ 

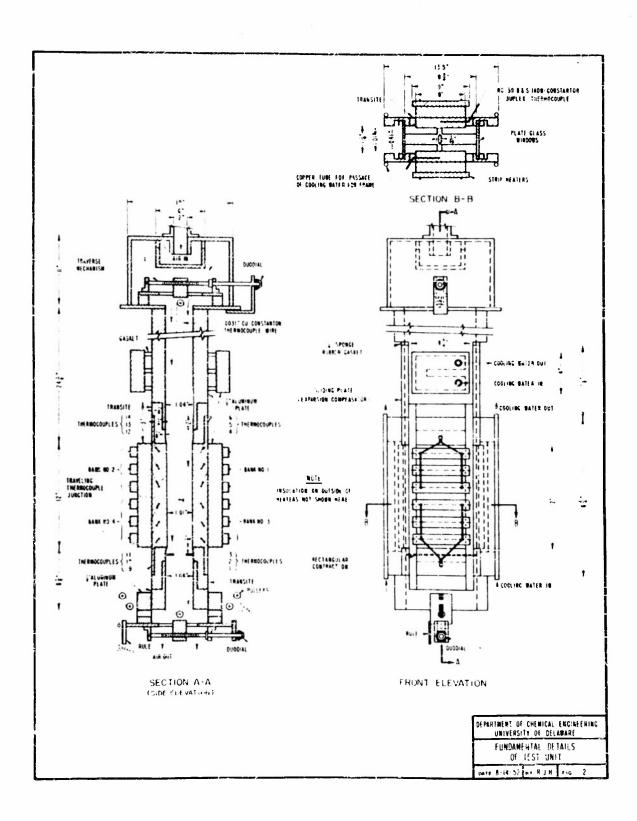
TABLE AV

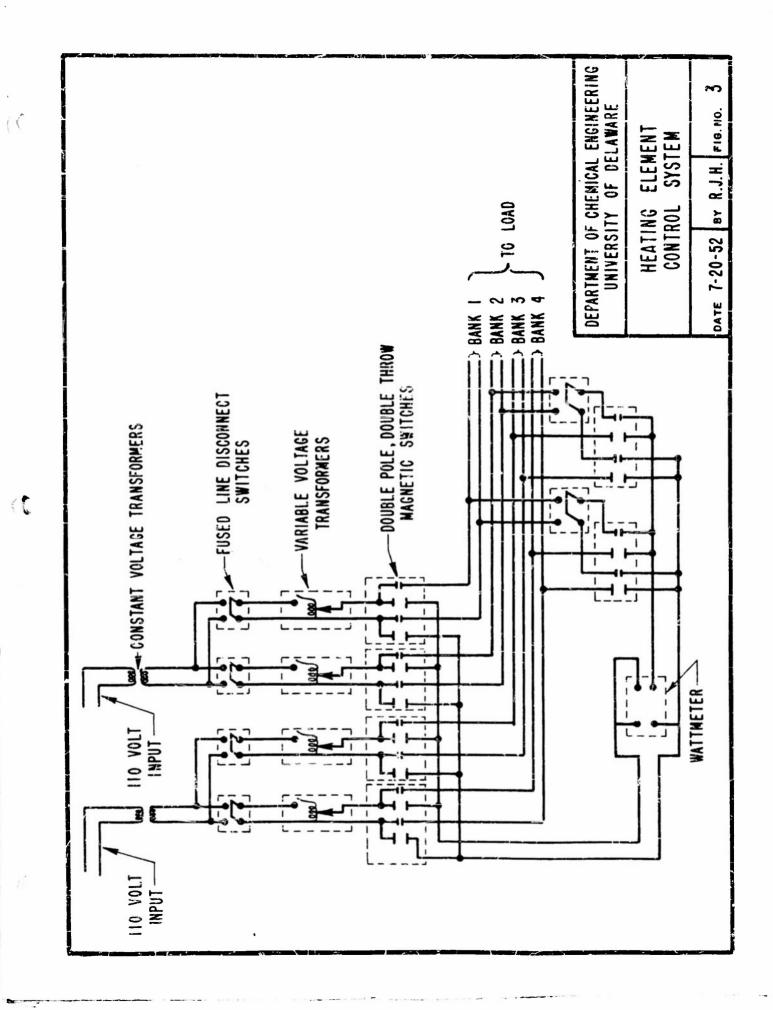
CENTER-LINE CORE TEMPERATURE, \* OF

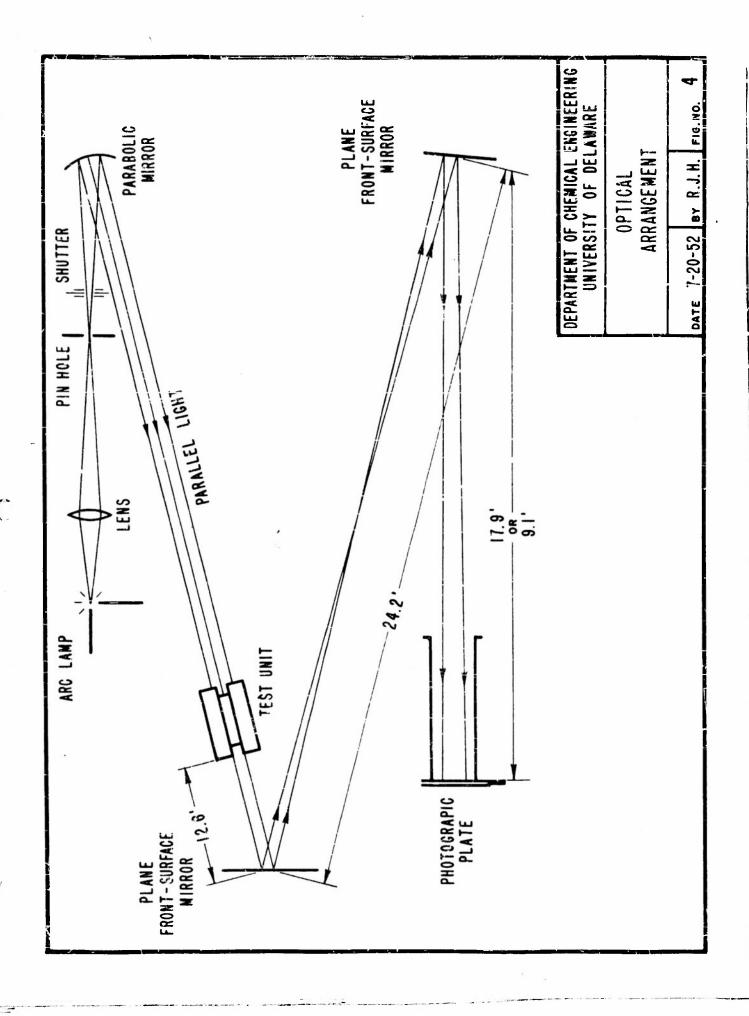
RUN NO.		Distar	ice from	the top,	, x, inch	ies	
	0	11	3	6	9	11	11 3/4
A-1	83.5	33.5	90.5	100.9	124.9	130.9	134.6
A-2	86.3	90.5	122.6	140.1	153.4	176.0	177.6
A-3	99.7	104.3	138.1	189.5	220.5	238.6	240.1
A-4	107.3	120.6	175.3	220.7	250.7	293.4	302.5
X-4	89.1	90.3	108.5		211.9	221.6	233.8
B-1b	100.9	101.3	102.0	103.6	106.2	109.9	109.3
B-2b	103.4	103.7	104.5	107.8	118.2	124.6	127.1
B-3	91.1	91.5	93.6	103.2	126.4	151.7	159.2
B-4	93.9	94.7	96.8	111.7	171.4	192.6	201.3
0-1b	106.5	106.6	106.7	107.3	109.1	109.9	110.5
0-2b	105.2	105.6	105.8	108.0	110.9	115.4	116.3
0-3a	96.8	97.1	98.0	102.3	114.4	121.7	123.4
0-3b	104.1	104.3	105.1	108.6	116.9	124.6	126.0
0-4	103.6	104.5	105.8	110.7	122.6	140.5	143.1
D-16	109.0	108.9	109.0	109.4	110.6	111.4	112.2
D-2	100.2	100.2	100.3	102.0	104.9	107.4	109.4
D-3	98.5	98.5	99.1	102.4	108.7	115.9	118.9
D-4	111.4	112.3	113.3	118.2	126.0	135.3	137.5
E-1	108.8	108.6	108.6	109.0	110.8	111.8	112.5
E-2	108.4	108.2	108.8	110.6	113.6	116.9	117.2
E-3	104.3	104.3	104.8	107.4	112.2	116.7	118.4
E-4	102.6	103.3	104.7	108.2	115.6	121.9	125.9

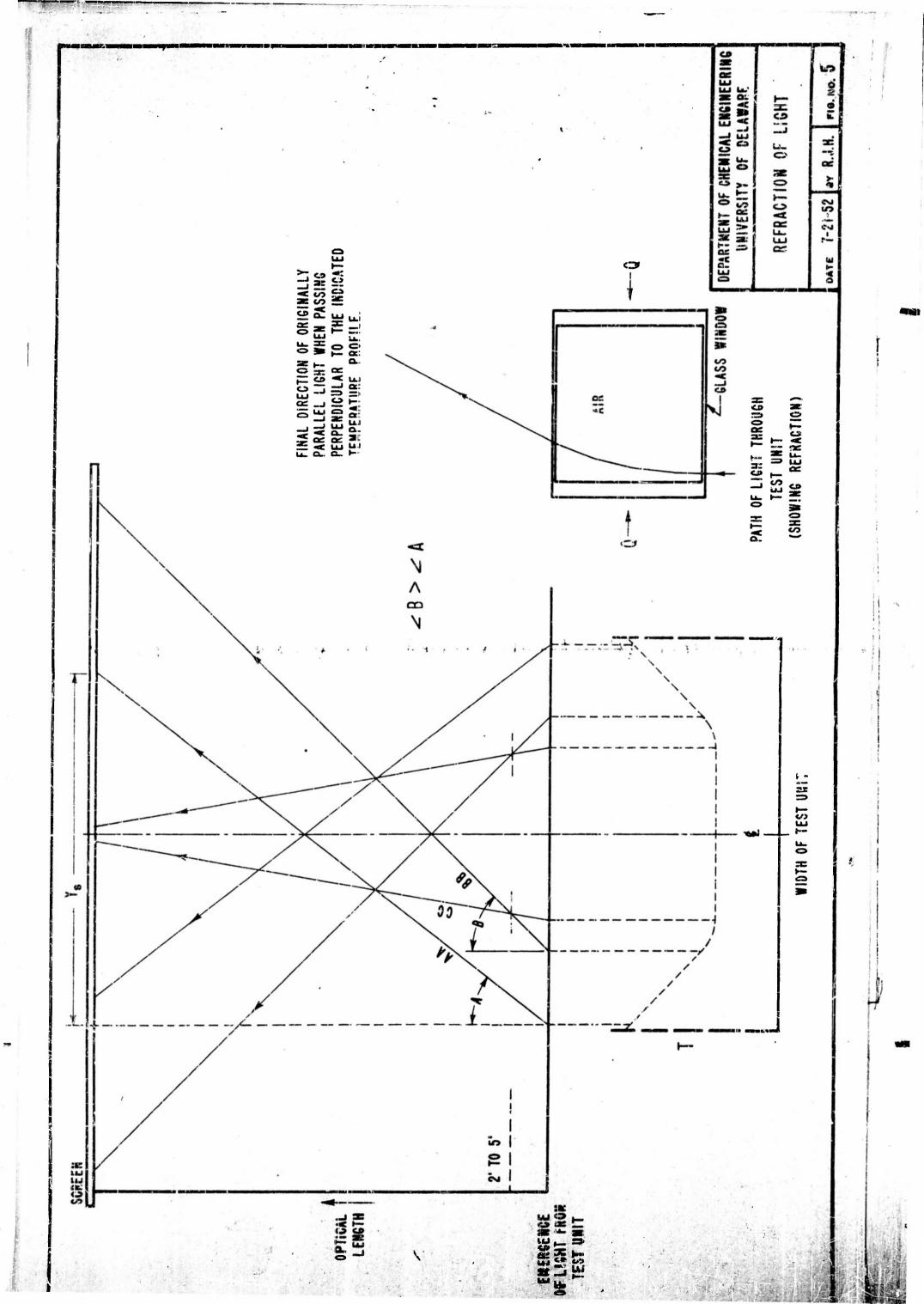
<sup>#</sup> All Temperatures are in or.











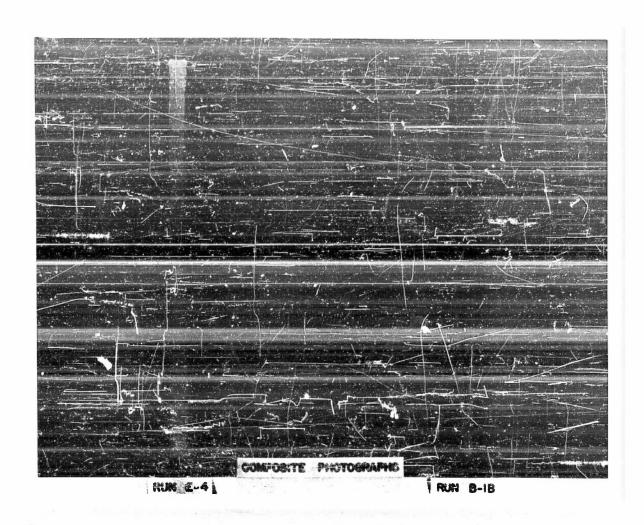
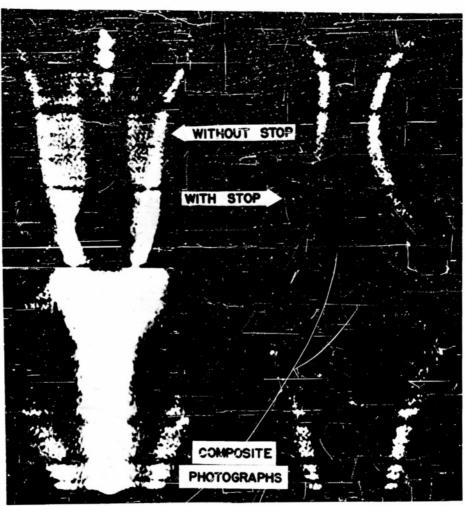


Figure 6. Composite shadowgraphs of runs in which the upward buoyant effect is not noticeable.

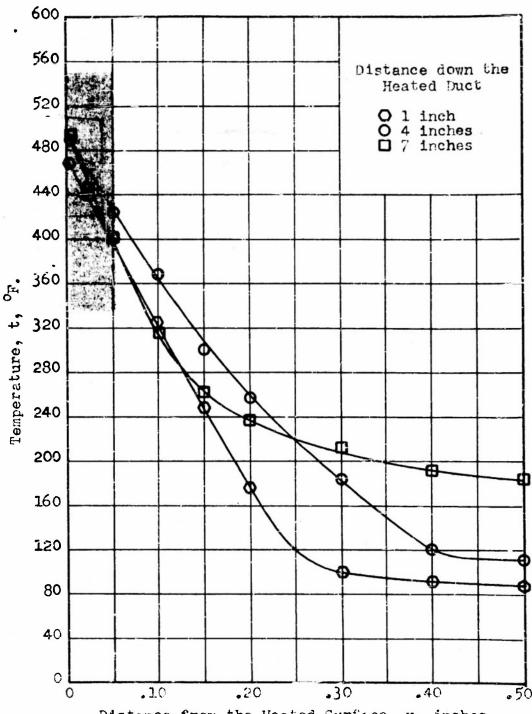


RUN X-4

Figure 7. Composite shadowgraphs of Run X-4 in which the apward buoyant effect is noticable.



Figure 8. Short-range shadowgraphs of Run X-4. Lowest horizontal bar on the upper heating section photo (left) is at the same position in the test unit as the highest bar on the lower heating section photo (right).



Distance from the Heated Surface, y, inches Figure 9. Temperature versus Distance from the Heated Surface at Various Distances Down the Heated Duct in Run X-4.

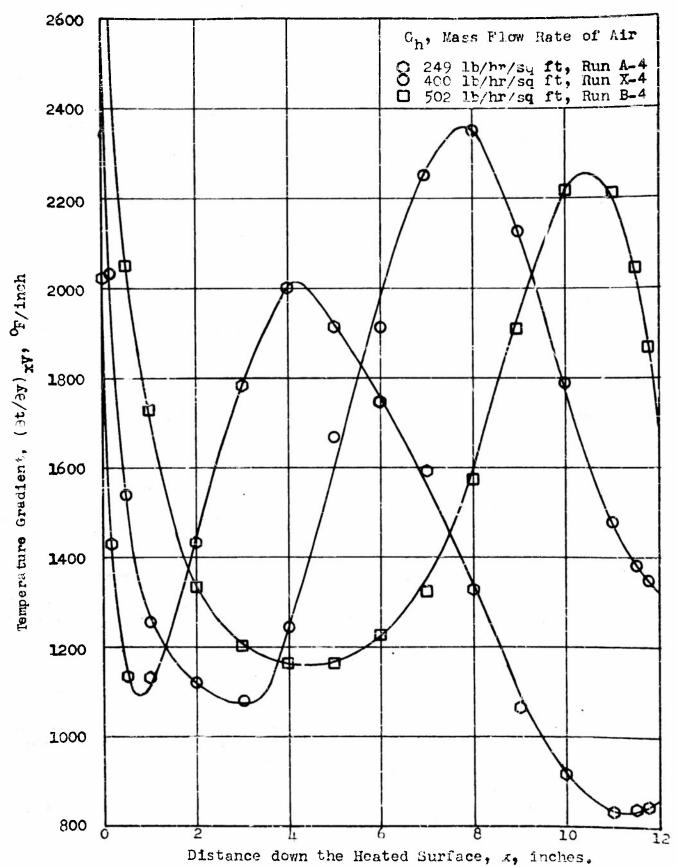


Figure 10. Variation of Air Temperature Gradient at the Wall versus Distance down the Heated Surface at Various Flow Rates and Constant Average Wall Temperature



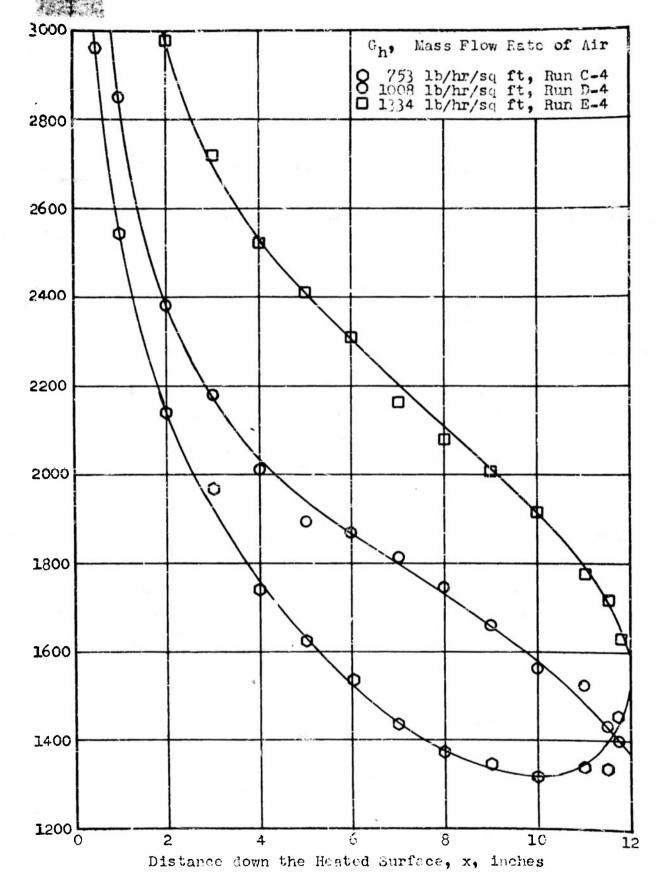
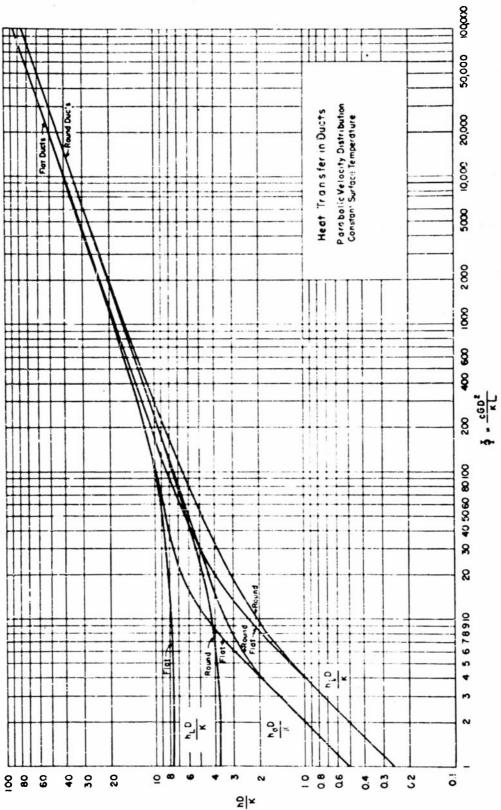


Figure 11. Variation of Air Temperature Gradient at the Wall versus Distance down the Heated Surface at Various Flow Rates and Constant Average Wall Temperatures.



RESULTS SHOWN ON THEORETICAL HEAT-TRANSFER CCARELATION FOR LAMINAR FLOW IN BOTH FLAT AND ROUND DUCTS; LOGARITHMIC-MEAN, ARITHMETIC-MEAN, AND INLET-TEMPERATURE-DIFFERENCE BASES

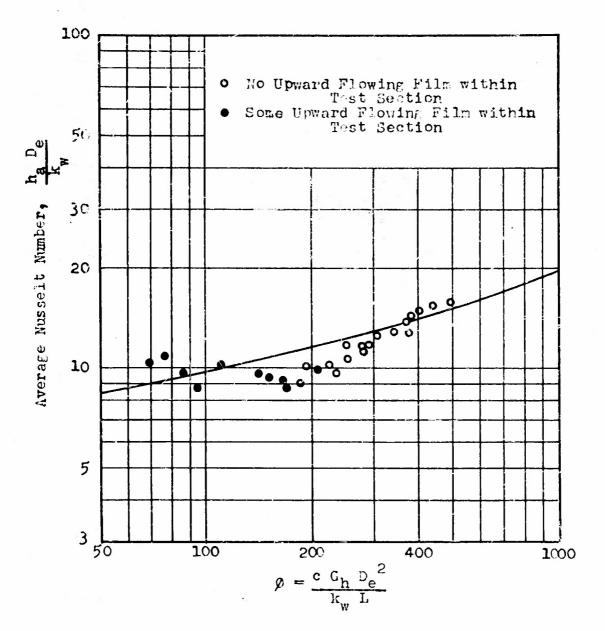


Figure 13. Comparison of Experimental Data of the One Foot Heated Length of Duct with the Theoretical Expression (solid line).

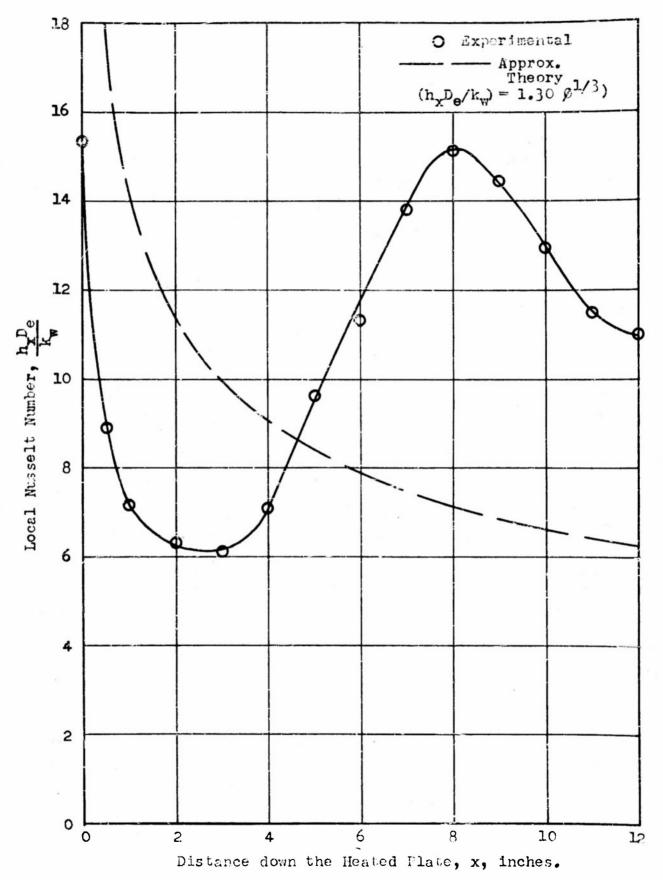
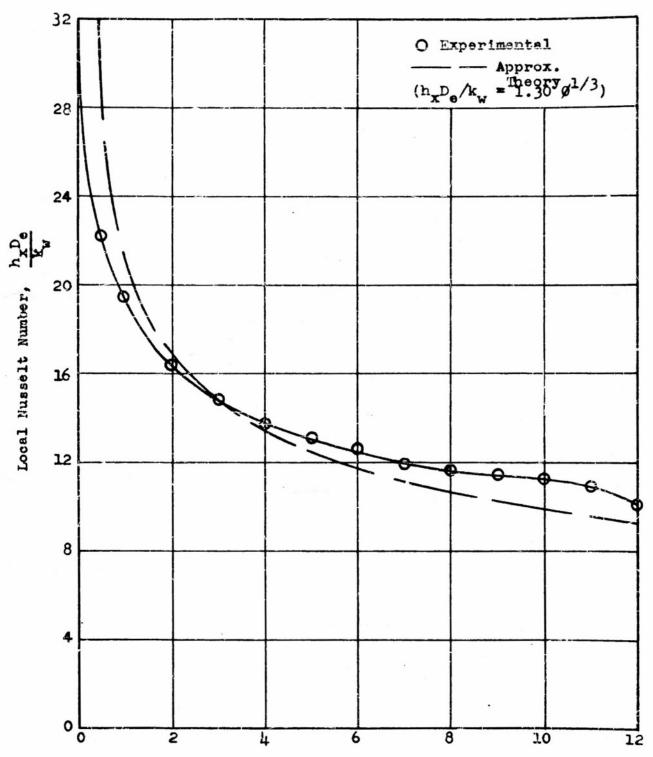


Figure 14. Comparison of Local Nusselt Number with Distance down the Heated Surface for Run X-4.



Distance down the Heated Plate, x, inches.

Figure 15. Comparison of Local Nusselt Number with
Distance down the Heated Surface for Run E-4.

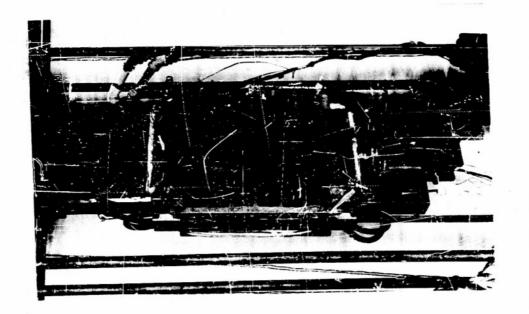


Figure 16. Complete test unit.



Figure 18. Heated section of test unit without heating Jements.

Figure 17. Heated section of test unit showing heating elements.



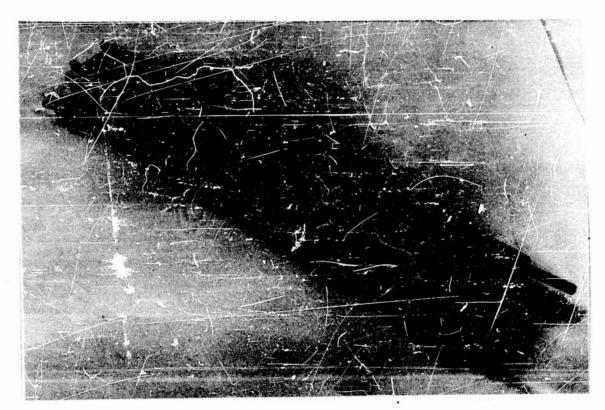


Figure 19. Window frame showing flush nature of glass with the end wall.

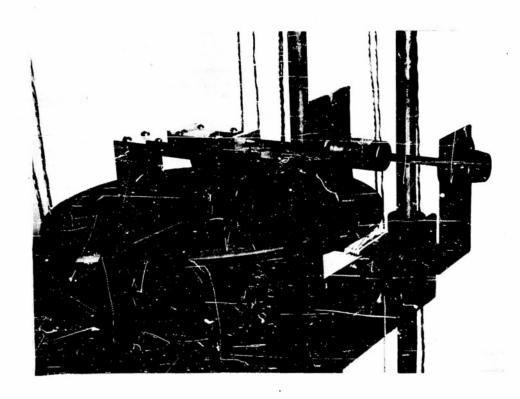


Figure 20. Top Traverse Mechanism

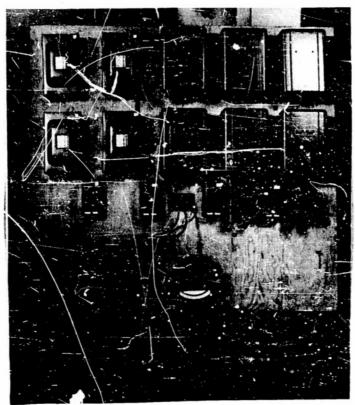


Figure 21. Control Board